

ECE 3318

Applied Electricity and Magnetism

Spring 2023

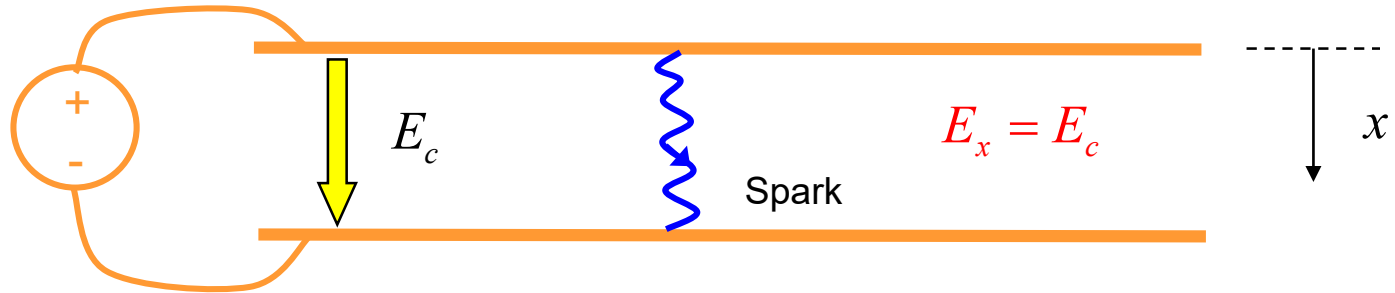
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Dept. of ECE



Notes 22
Dielectric
Breakdown

Dielectric Breakdown

1 Arcing (spark)



Parallel-plate capacitor with uniform electric field

E_c = “critical electric field”

The air ionizes and “runaway” (avalanche) breakdown occurs

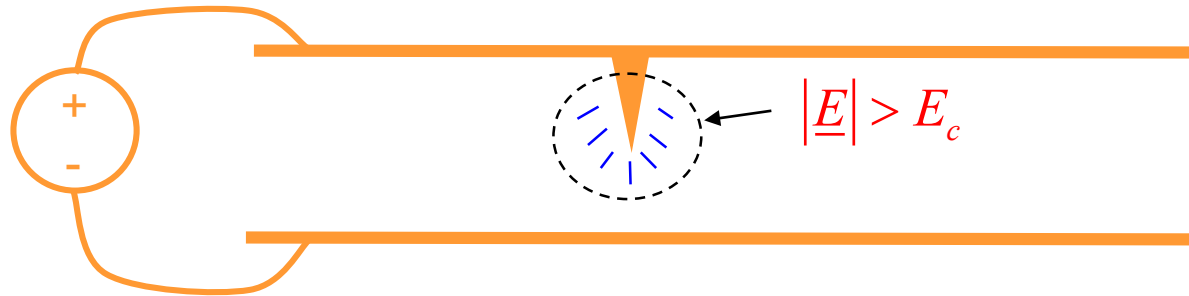
Air : $E_c = 3 \times 10^6$ [V/m]

Oil : $E_c = 15 \times 10^6$ [V/m]

Glass : $E_c = 30 \times 10^6$ [V/m]

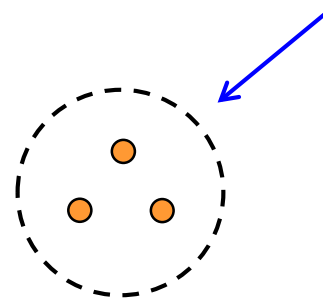
Dielectric Breakdown (cont.)

2 Corona Discharge (local breakdown)



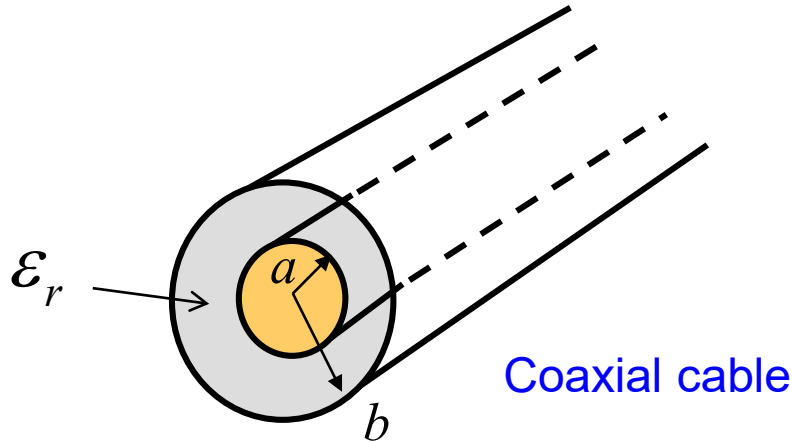
400 kV high-voltage transmission line near Madrid, Spain (Wikipedia)

Bundled conductors tend to act like one larger conductor in terms of the breakdown.



Power lines are often grouped together (“bundled conductors”) to reduce conductor losses and the corona effect.

Example



$$\epsilon_r = 2.0$$

$$E_c = 15 \times 10^6 \text{ [V/m]}$$

$$b = 0.25 \text{ [cm]}$$

$$a = 0.5 \text{ [mm]}$$

Find: V_{\max} (assume a safety factor SF = 2)

At breakdown:

$$\underline{E}^{\max}(\rho) = \underline{\hat{\rho}} \left(\frac{\rho_l^{\max}}{2\pi\epsilon_0\epsilon_r\rho} \right)$$

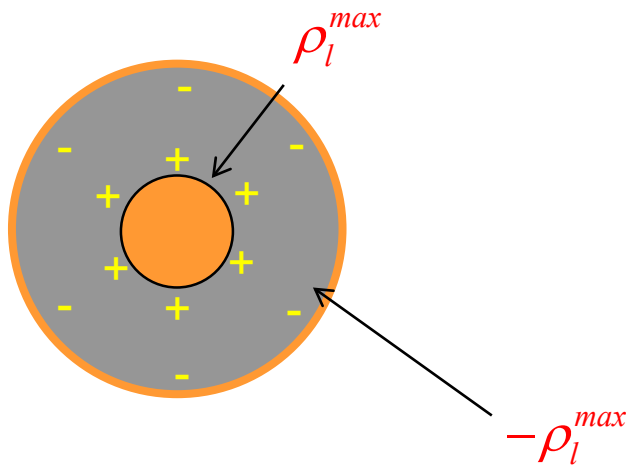
Set $\rho = a$ (breakdown occurs here first):

$$E_{\rho}^{\max}(a) = E_c = \frac{\rho_l^{\max}}{2\pi\epsilon_0\epsilon_r a}$$

Note:

$$\rho_{sa}^{\max} = \frac{\rho_l^{\max}}{2\pi a}$$

$$\rho_{sb}^{\max} = \frac{-\rho_l^{\max}}{2\pi b}$$



Example (cont.)

Thus $\rho_l^{\max} = 2\pi\epsilon_0\epsilon_r a E_c$

Hence $\underline{E}^{\max}(\rho) = \underline{\hat{\rho}} \left(\frac{\rho_l^{\max}}{2\pi\epsilon_0\epsilon_r\rho} \right) \rightarrow \underline{E}^{\max}(\rho) = \underline{\hat{\rho}} E_c \left(\frac{a}{\rho} \right)$

We then have
$$\begin{aligned} V_{\max} = V_{AB} &= \int_A^B \underline{E}^{\max} \cdot \underline{dr} = \int_a^b E_{\rho}^{\max} d\rho \\ &= \int_a^b E_c \left(\frac{a}{\rho} \right) d\rho \\ &= E_c a \ln \rho \Big|_a^b \end{aligned}$$

or

$$V_{\max} = E_c a \ln \left(\frac{b}{a} \right)$$

Example (cont.)

With safety factor:

Larger coaxes (larger a) can handle more voltage and power.

$$V_{\max}^{\text{SF}} = \left(\frac{1}{\text{SF}} \right) E_c a \ln \left(\frac{b}{a} \right)$$
$$= \left(\frac{1}{2} \right) \left(15 \times 10^6 \left(0.5 \times 10^{-3} \right) \ln(5) \right)$$

$$V_{\max}^{\text{SF}} = 6035.4 \text{ [V]}$$

Example (cont.)

Power flowing down the line: Phasor domain voltage

$$P_{\max}^{\text{SF}} = \frac{1}{2} \frac{|V_{\max}^{p,\text{SF}}|^2}{Z_0} \quad (\text{from ECE 3317})$$

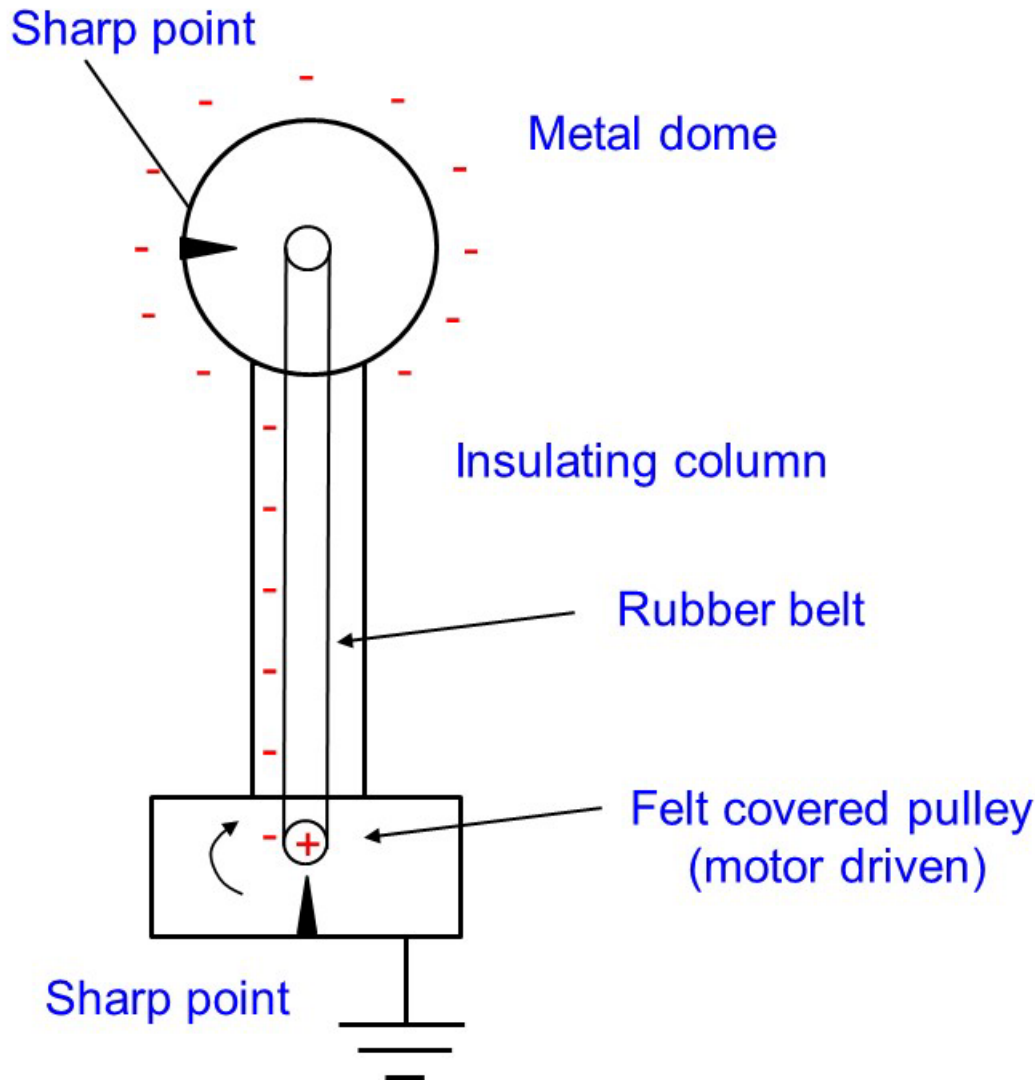
$$Z_0 = \frac{\eta_0}{2\pi\sqrt{\epsilon_r}} \ln\left(\frac{b}{a}\right) \quad [\Omega] \quad (\text{derived later})$$

$$Z_0 = 68.3 \quad [\Omega]$$

This gives us

$$P_{\max}^{\text{SF}} = 2.67 \times 10^5 \quad [\text{W}]$$

Van de Graaff Generator



Principles:

- (1) Electric field is high near sharp points: air is ionized and charges are free to jump on/off.
- (2) Faraday cage effect: No matter how much charge is placed on the dome, it goes to the outside and there is little field on the inside.

The felt on the bottom pulley becomes positively charged.

Van de Graaff Generator (cont.)



Dr. Robert J. Van de Graaff (1901-1967) was a professor at Princeton university and a Research Associate at MIT. The Van de Graaff generator was invented in 1929 and originally used as a research tool in early atom-smashing and high energy X-ray experiments.

Van de Graaff Generator (cont.)



This picture shows Dr. Van de Graaff with his first generator (80 [kV]).

Van de Graaff Generator (cont.)



Inside each dome
there was a laboratory.

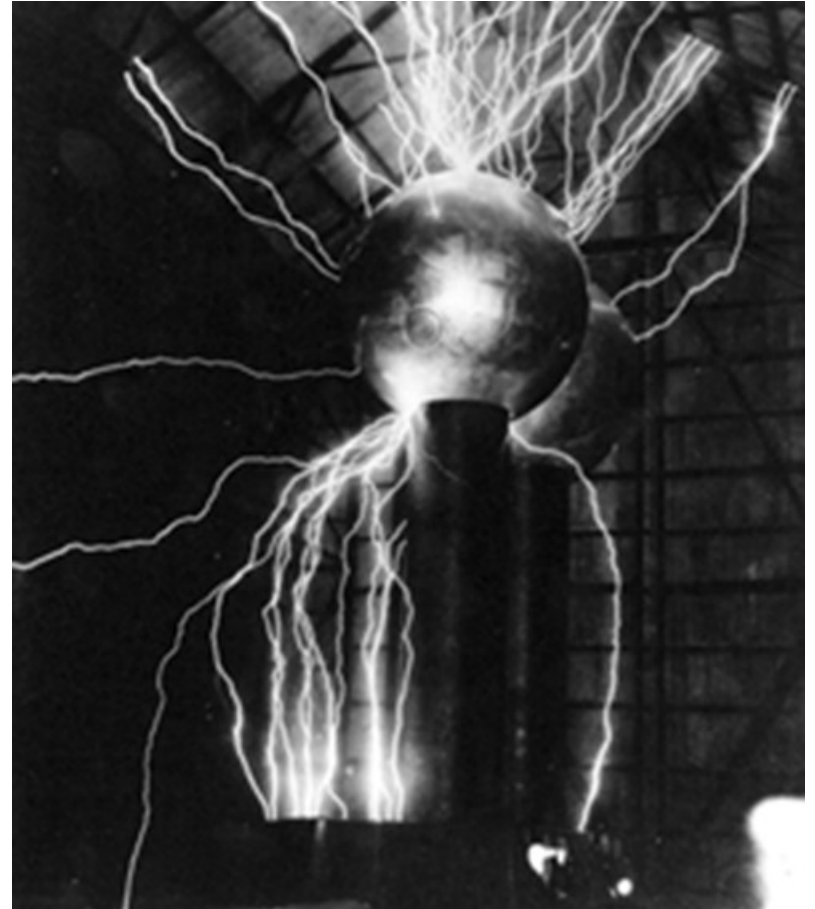
The world's largest air-insulated Van de Graaff generator, designed and built by Van de Graaff during 1931-1933. The spheres are 15 feet in diameter and 43 feet off the ground. It can produce 7 [MV].

Van de Graaff Generator (cont.)

In the early 1950's, the giant Van de Graaff generator was donated to the **Boston Museum of Science**.

For years, it was enclosed in a small steel structure on the Museum's property, where it was occasionally demonstrated.

Finally, in 1980, the **Thomson Theatre of Electricity** was completed inside the museum. The generator is demonstrated at least twice daily, to teach public and school audiences about electricity and lightning.



Van de Graaff Generator (cont.)

Boston Museum of Science



Van de Graaff Generator (cont.)



A modern Van de Graaff generator integrated with a particle accelerator. The generator produces the high voltages (in the megavolt range) that accelerates particles.

(from Wikipedia)

Van de Graaff Generator (cont.)

For more information:

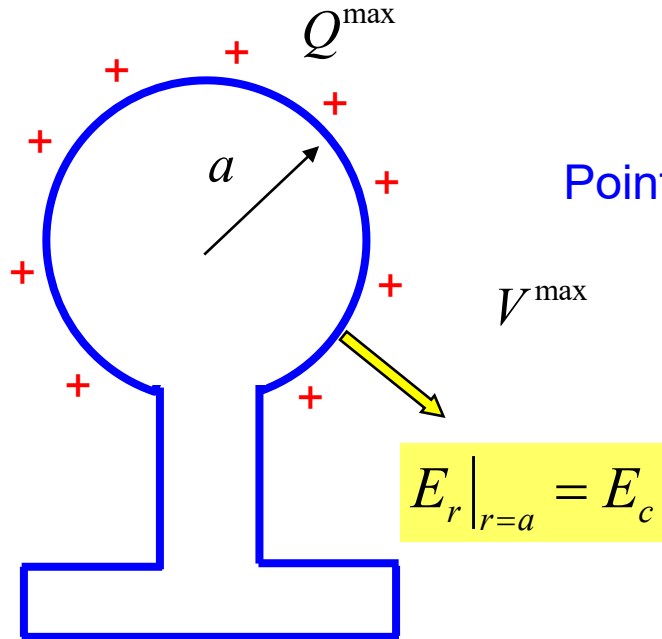
http://en.wikipedia.org/wiki/Van_de_Graaff_generator

Van de Graaff Generator (cont.)

Find the maximum voltage V_{\max} on a Van de Graaff Generator in air

Point charge electric field formula: $\frac{Q_{\max}}{4\pi\epsilon_0 a^2} = E_c$

$$\Rightarrow Q_{\max} = 4\pi\epsilon_0 a^2 E_c$$



Point charge potential formula: $\Phi^{\max}(r) = \frac{Q_{\max}}{4\pi\epsilon_0 r}$

$$V_{\max} = \Phi^{\max}(a) = \frac{Q_{\max}}{4\pi\epsilon_0 a} = \frac{4\pi\epsilon_0 a^2 E_c}{4\pi\epsilon_0 a}$$

Hence

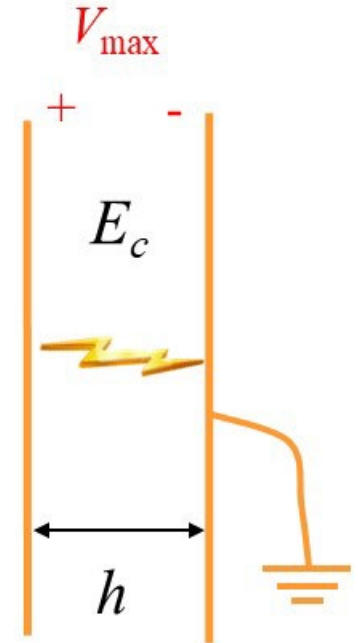
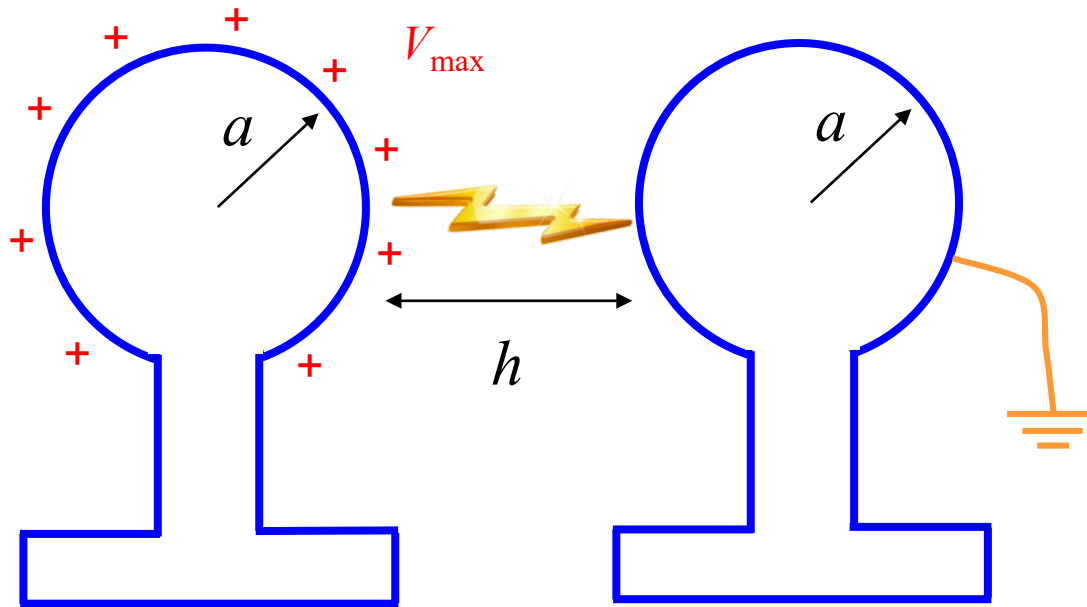
$$V_{\max} = a E_c$$

(Assume zero volts at infinity.)

A bigger dome can support a higher voltage!

Van de Graaff Generator (cont.)

Find the maximum spark length to a grounded sphere



$$V_{\max} \approx E_c h \text{ (parallel-plate approximation)}$$

$$\Rightarrow h = \frac{V_{\max}}{E_c} = \frac{E_c a}{E_c} = a$$

$$h = a$$

$$V_{\max} = E_c h$$

The spheres are approximated as flat conductors.

Van de Graaff Generator (cont.)

Example

Assume

$$a = 0.1 \text{ [m]}$$

$$E_c = 3 \times 10^6 \text{ [V/m]}$$

Note:

This dimension corresponds to the small Van de Graaff that we have in the ECE Department.

$$V_{\max} = 300,000 \text{ [V]}$$

Maximum voltage

$$h = 0.1 \text{ [m]} \quad (h = 3.9 \text{ [inches]})$$

Spark length

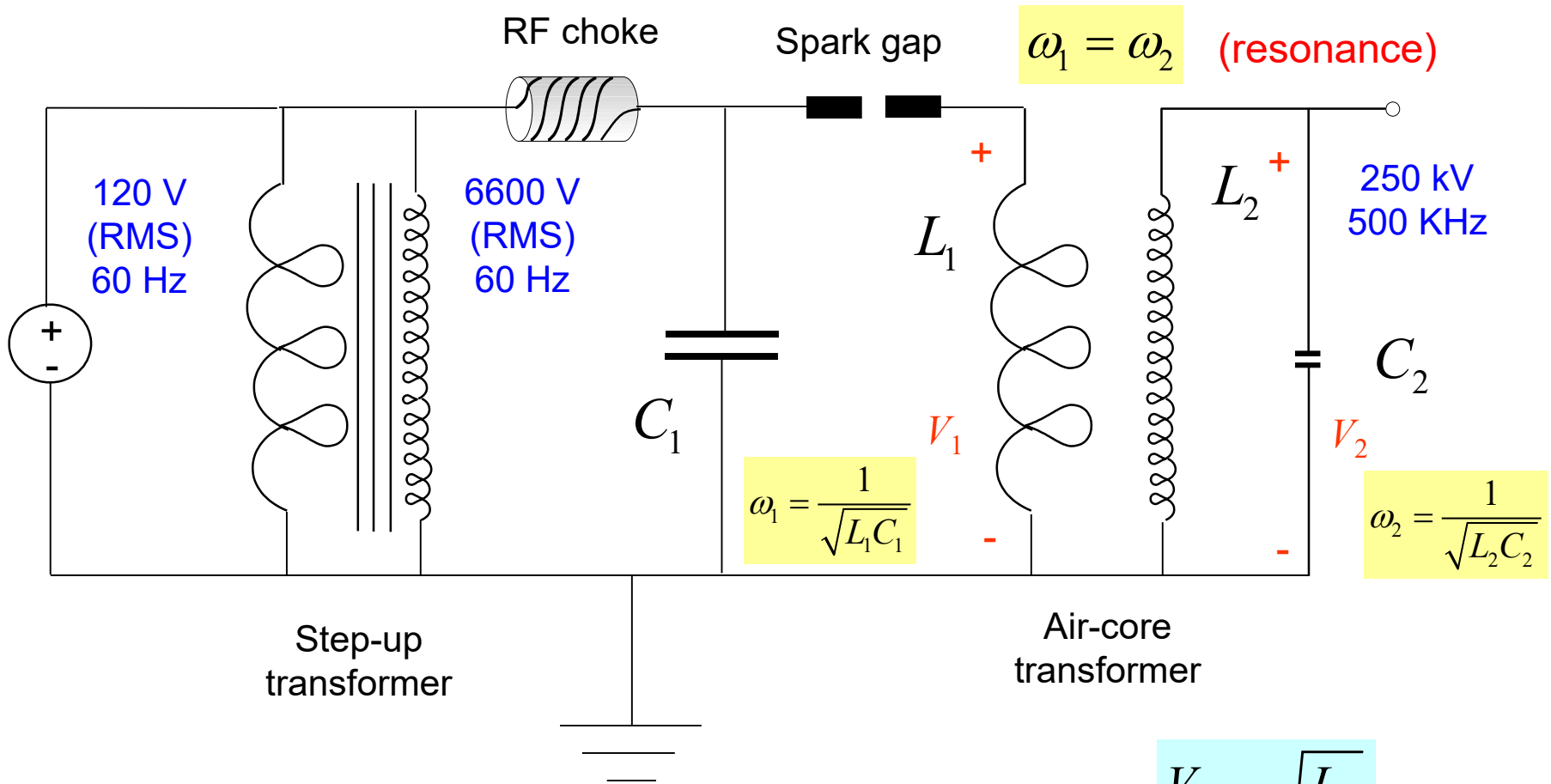
Tesla Coil

This is used to produce high voltage at AC (typically about 1 [MHz]).



Tesla Coil (cont.)

Equivalent circuit for a typical Tesla coil
 (“resonant air-core transformer”)



Output: 250 kV at 500 kHz
 (Tesla coil in our lab)

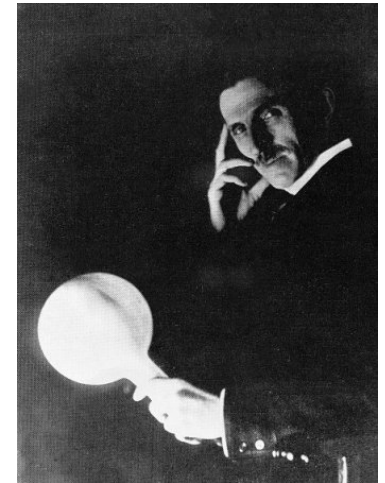
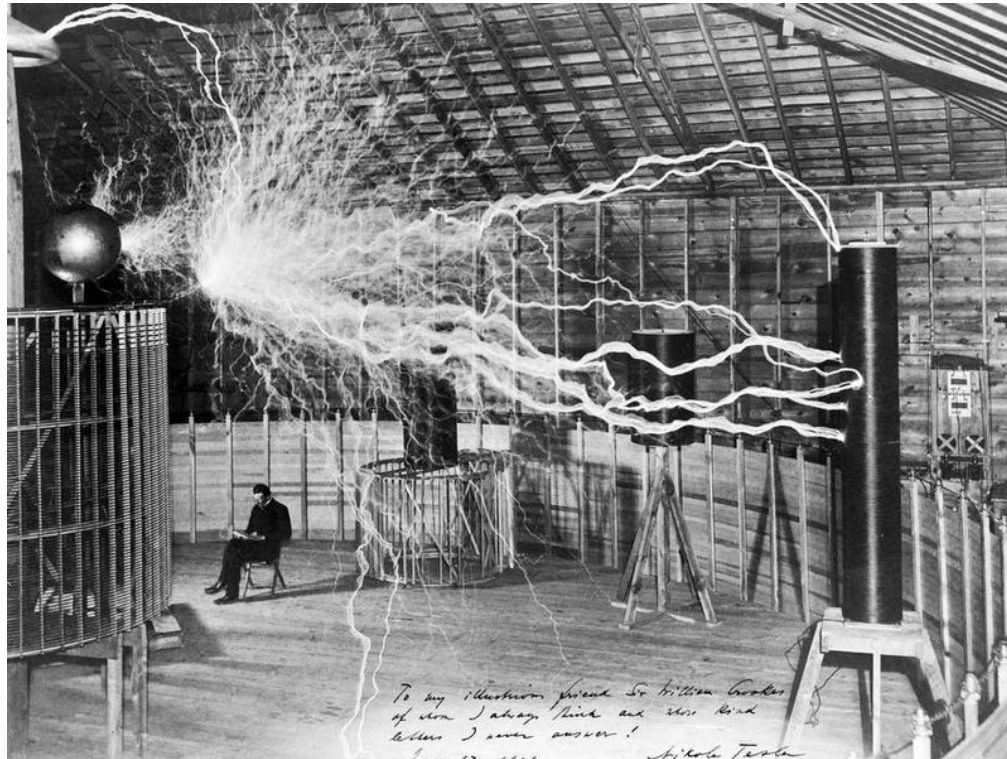
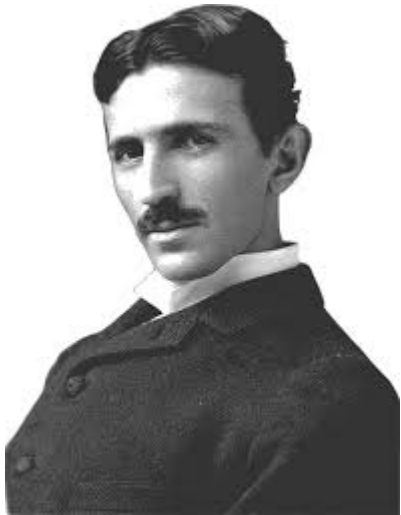
At resonance:

$$\frac{V_2}{V_1} = \sqrt{\frac{L_2}{L_1}}$$

Tesla Coil (cont.)

Pictures of Tesla:

(1) by himself; (2) in his lab with a Tesla coil; (3) lighting a lightbulb wirelessly.



Lightning



Lightning (cont.)



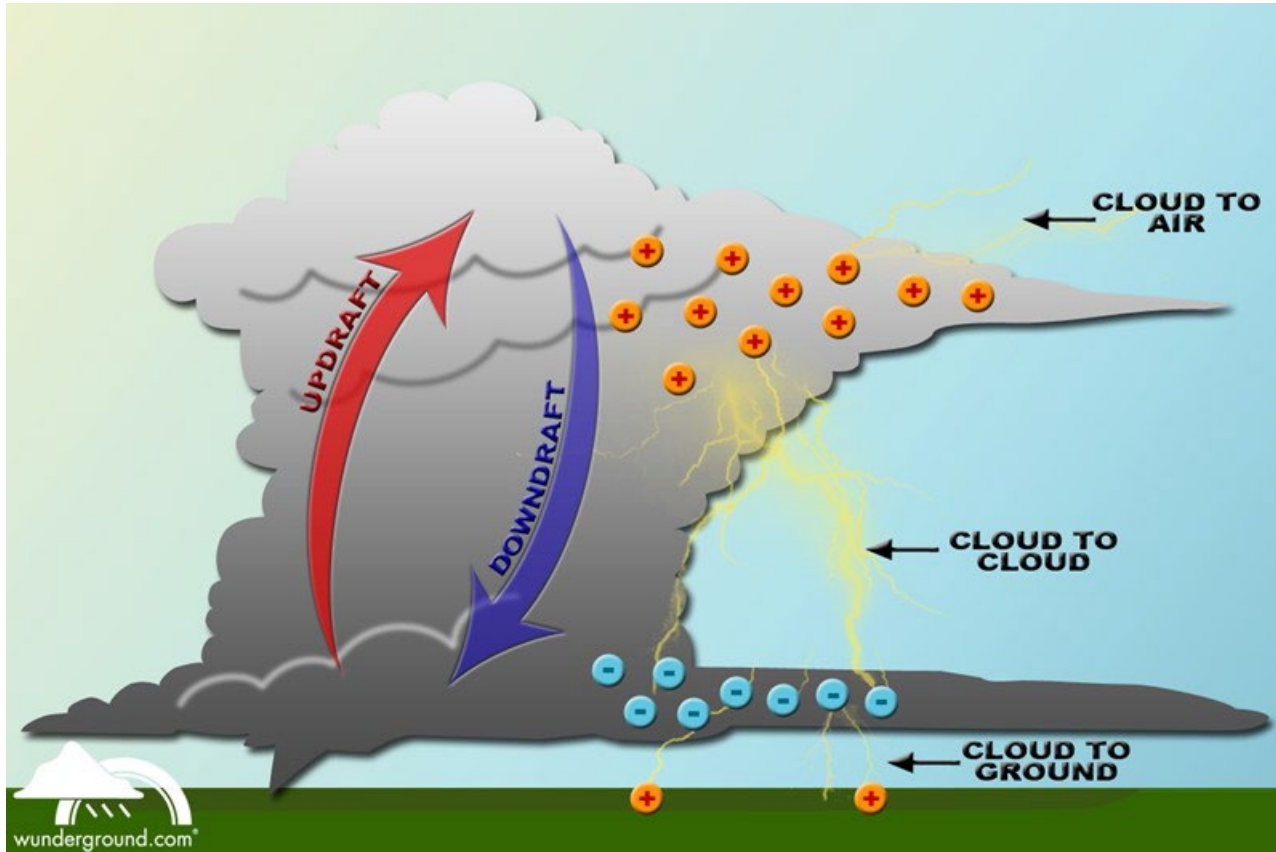
Lightning (cont.)



Lightning strikes at George Bush Intercontinental Airport, June 12, 2012.

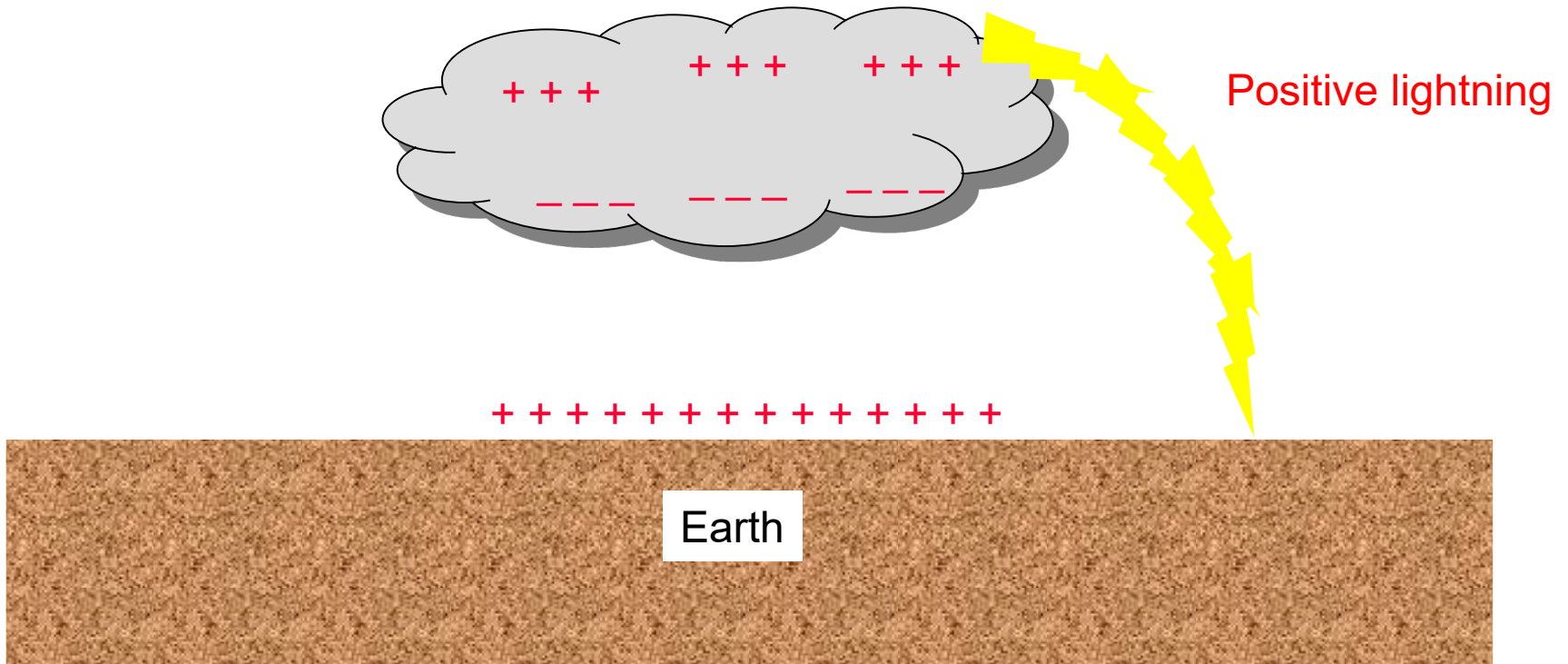
Credit: "texansgirl34"

Lightning (cont.)



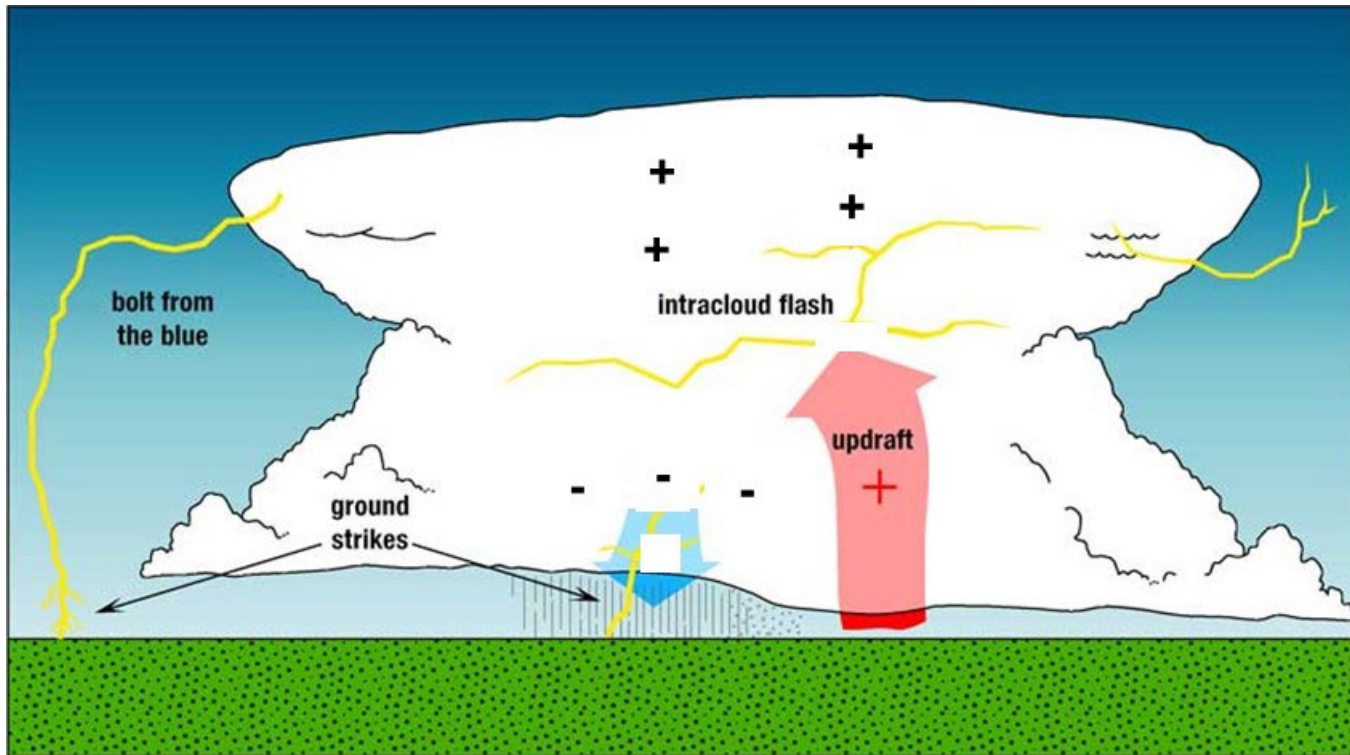
- Powerful air currents and friction between ice and water particles are believed responsible for the charge formation.
- The base of the thunder has negative charge and the top has positive charge (though there can be pockets of charge that are opposite).

Lightning (cont.)



Positive lightning can be up to 10 times as powerful as negative lightning: it can result in a “bolt from the blue,” striking miles away from the visible cloud (up to 25 miles away or more).

Lightning (cont.)



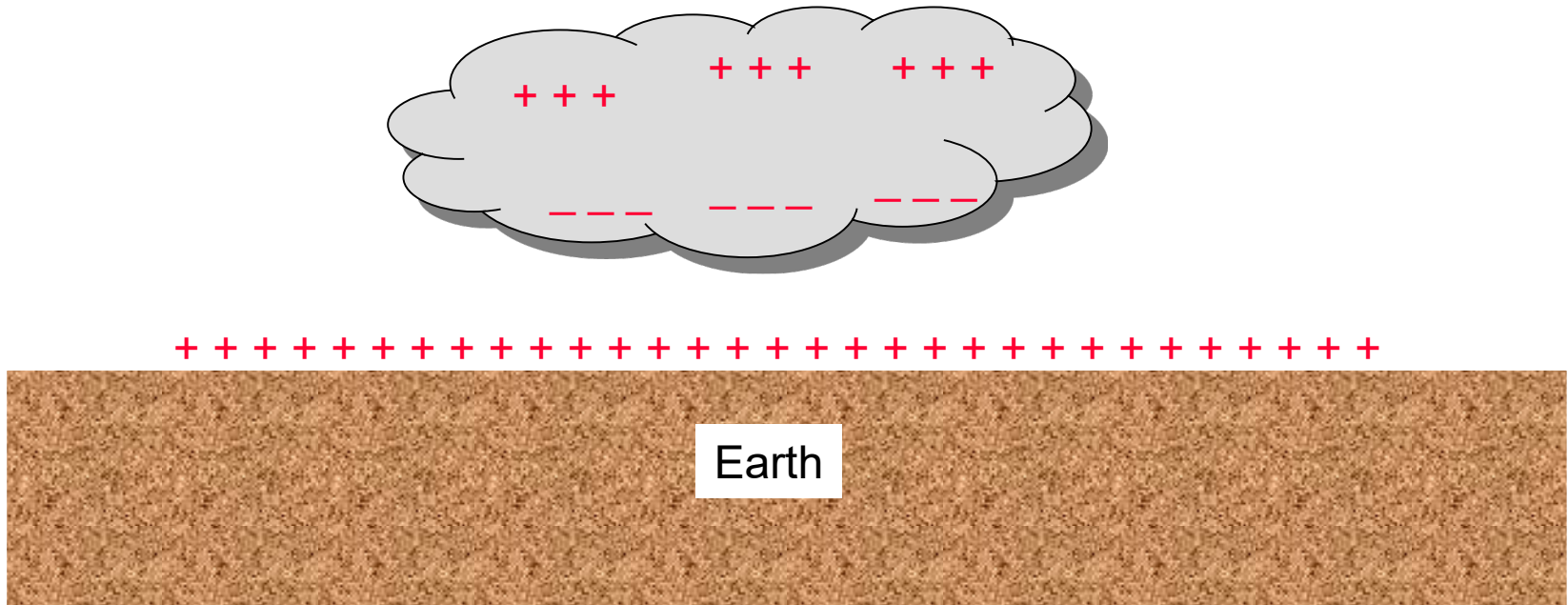
The different types of lightning that are usually observed are shown here.

Lightning (cont.)



Positive lightning (note that it originates from the top of the cloud).

Lightning (cont.)



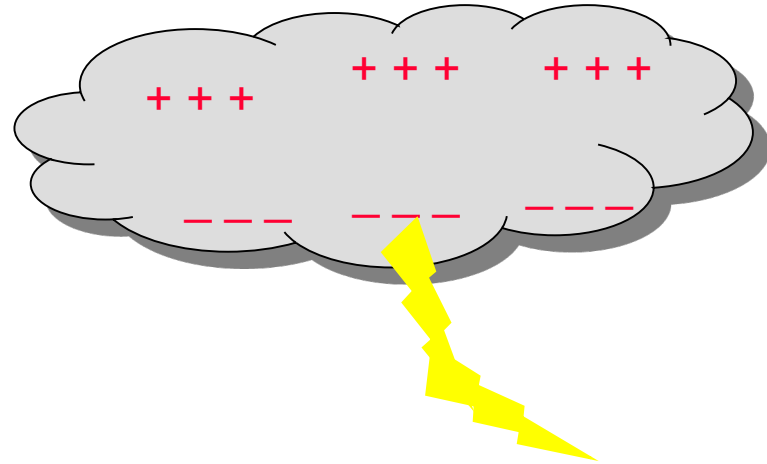
- ❖ The base of the thundercloud is typically at an altitude of about 1,500 [m]. The top of the thundercloud may be at about 10,000 [m] or higher.
- ❖ The voltage drop between the cloud base and ground is typically 150 [MV].

This is not nearly enough to arc from the cloud to ground!

$$E_c \approx 3.0 \text{ [MV/m]}$$

Lightning (cont.)

❖ A “stepped leader” begins descending from the cloud. It is a group of electrons that zigzags toward the earth. The charge is typically about -5 [C].



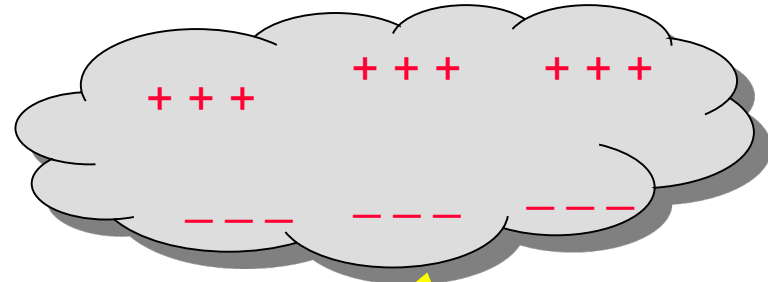
One theory is that cosmic rays are responsible for the formation of the leader, which ionize atoms and release electrons that get accelerated by the high electric fields.

- ❖ The stepped leader travels about 50 [m] in about 1 [μ s], then pauses for about 50 [μ s], and then continues, pausing every 50 [m] or so.
- ❖ The width of the leader channel is about 1.0 [cm].

The stepped leader does not “know” where it will strike until it is about 40 [m] or so from the earth.

Lightning (cont.)

❖ The stepped leader may branch as it descends (this is responsible for the forked appearance of most lightning).



Branches

+++++



Earth

Lightning (cont.)



Main channel

Branches

Lightning (cont.)

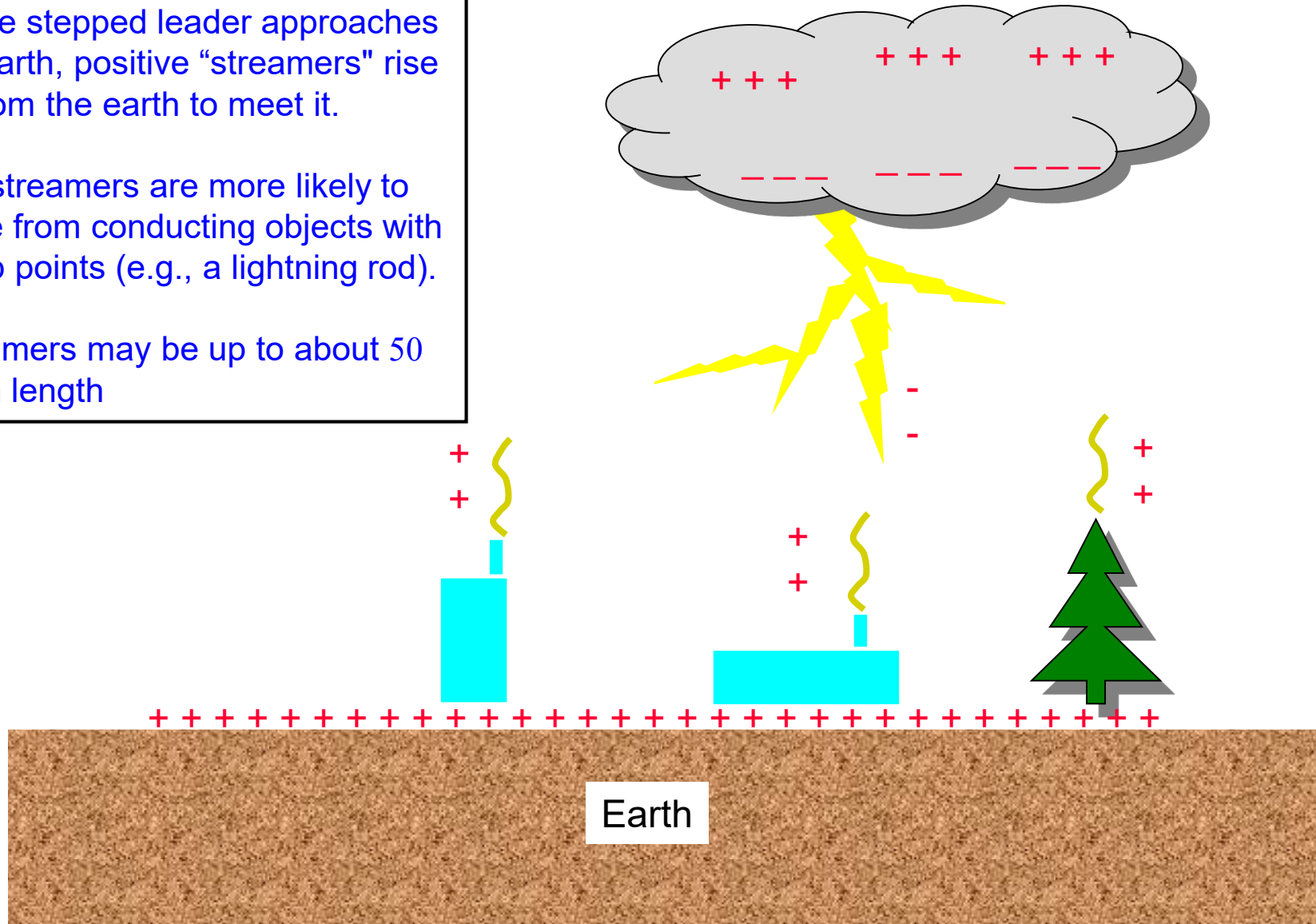


The pptx version has an animation (go to full-screen mode).

<http://en.wikipedia.org/wiki/Lightning>

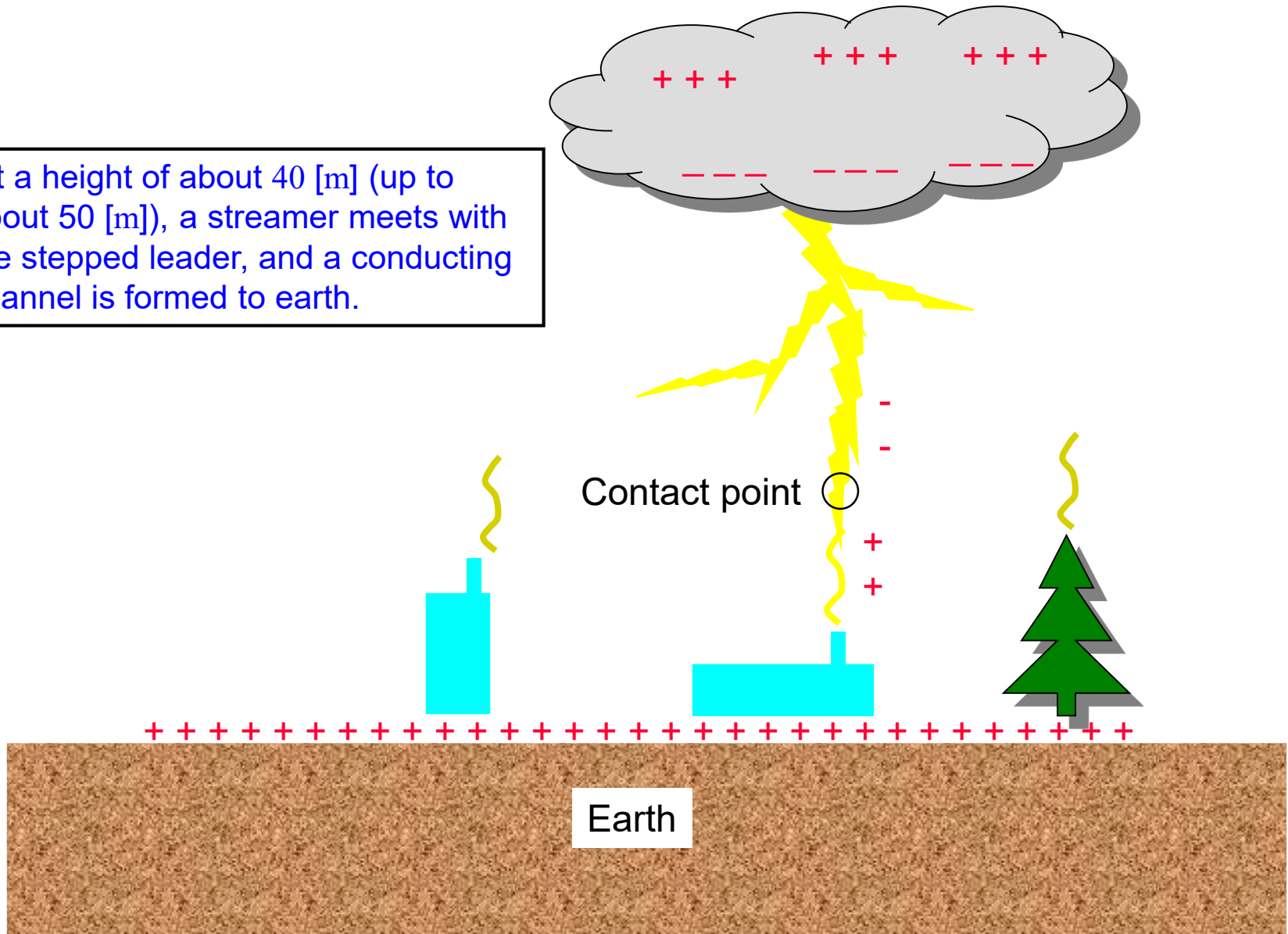
Lightning (cont.)

- ❖ As the stepped leader approaches the earth, positive “streamers” rise up from the earth to meet it.
- ❖ The streamers are more likely to come from conducting objects with sharp points (e.g., a lightning rod).
- ❖ Streamers may be up to about 50 [m] in length



Lightning (cont.)

❖ At a height of about 40 [m] (up to about 50 [m]), a streamer meets with the stepped leader, and a conducting channel is formed to earth.



Lightning (cont.)



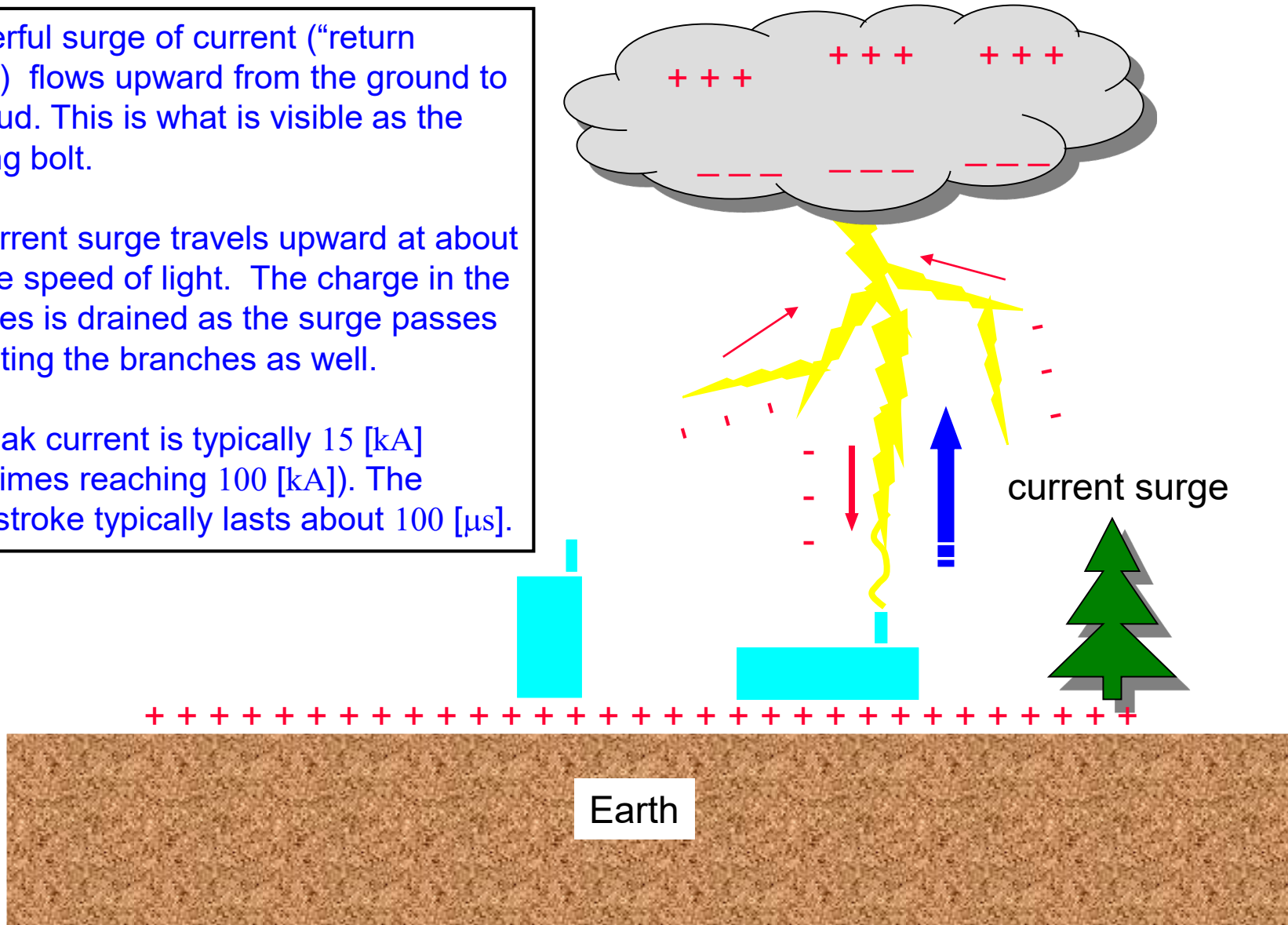
A lightning flash terminates
on a tree.

(An un-attached streamer is
visible on the earth surface
projection to the left.)

<http://en.wikipedia.org/wiki/Lightning>

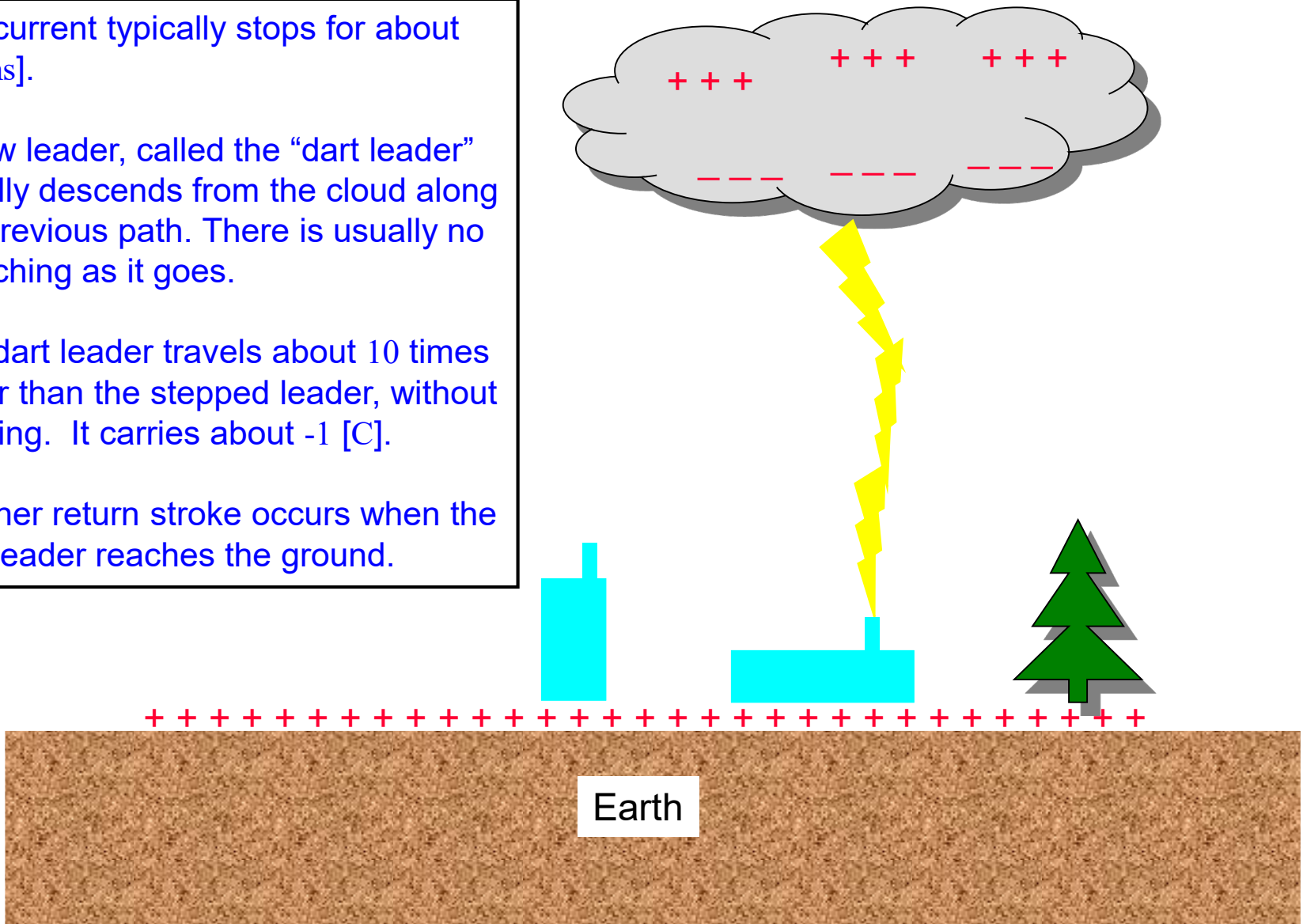
Lightning (cont.)

- ❖ A powerful surge of current (“return stroke”) flows upward from the ground to the cloud. This is what is visible as the lightning bolt.
- ❖ The current surge travels upward at about 25% the speed of light. The charge in the branches is drained as the surge passes by, lighting the branches as well.
- ❖ The peak current is typically 15 [kA] (sometimes reaching 100 [kA]). The return stroke typically lasts about 100 [μ s].



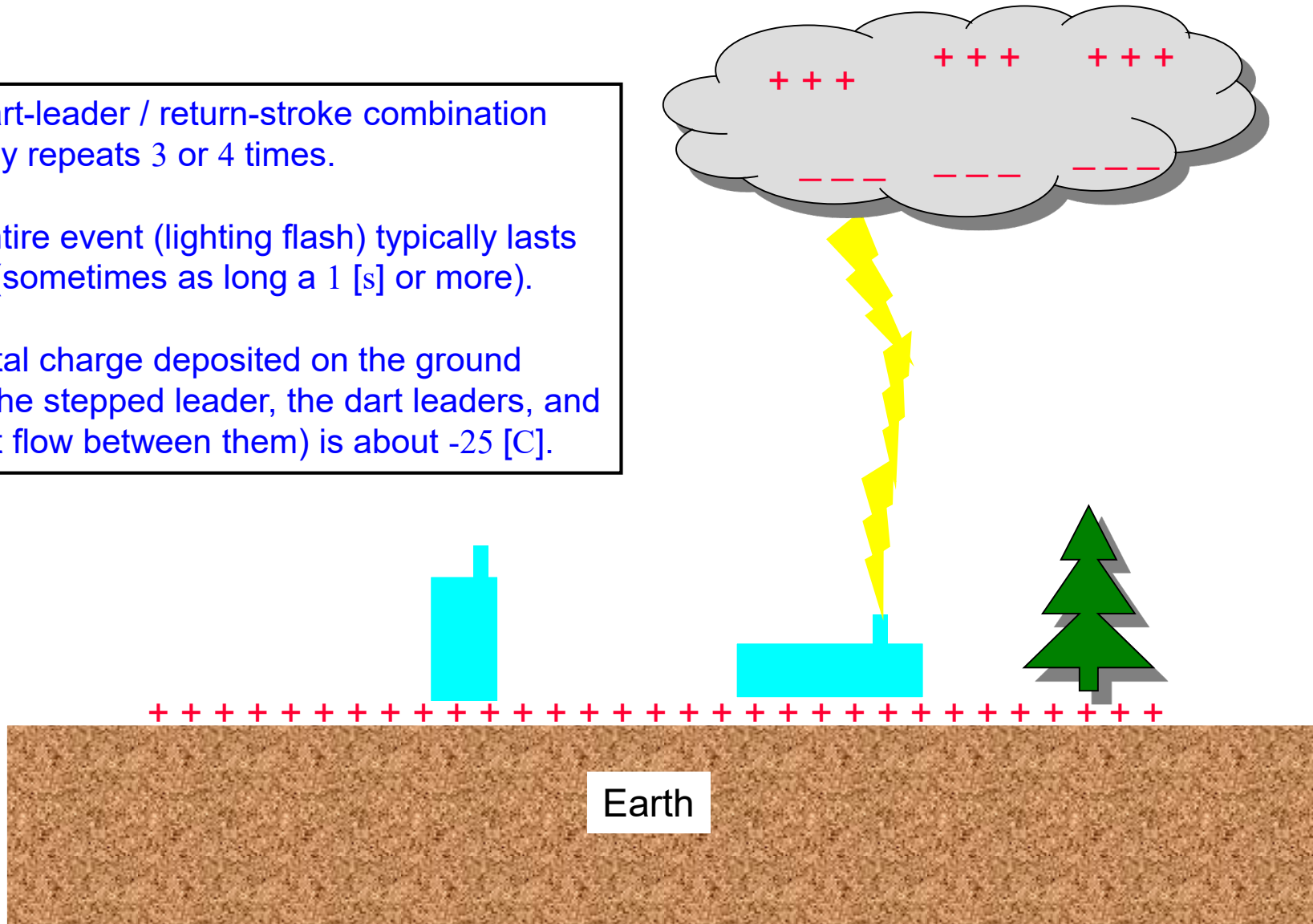
Lightning (cont.)

- ❖ The current typically stops for about 50 [ms].
- ❖ A new leader, called the “dart leader” usually descends from the cloud along the previous path. There is usually no branching as it goes.
- ❖ The dart leader travels about 10 times faster than the stepped leader, without pausing. It carries about -1 [C].
- ❖ Another return stroke occurs when the dart leader reaches the ground.



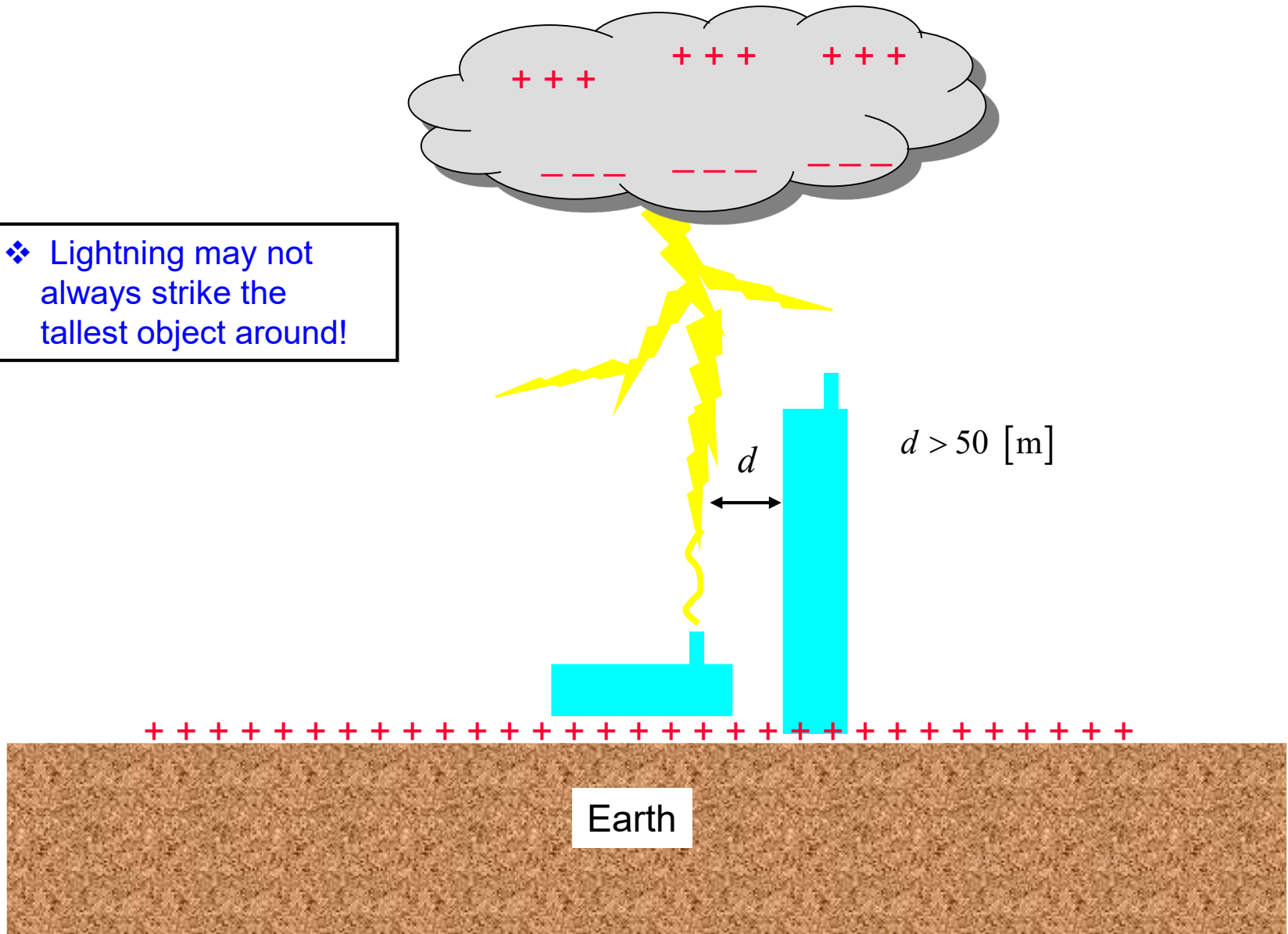
Lightning (cont.)

- ❖ The dart-leader / return-stroke combination typically repeats 3 or 4 times.
- ❖ The entire event (lighting flash) typically lasts 0.2 [s] (sometimes as long a 1 [s] or more).
- ❖ The total charge deposited on the ground (from the stepped leader, the dart leaders, and current flow between them) is about -25 [C].



Lightning (cont.)

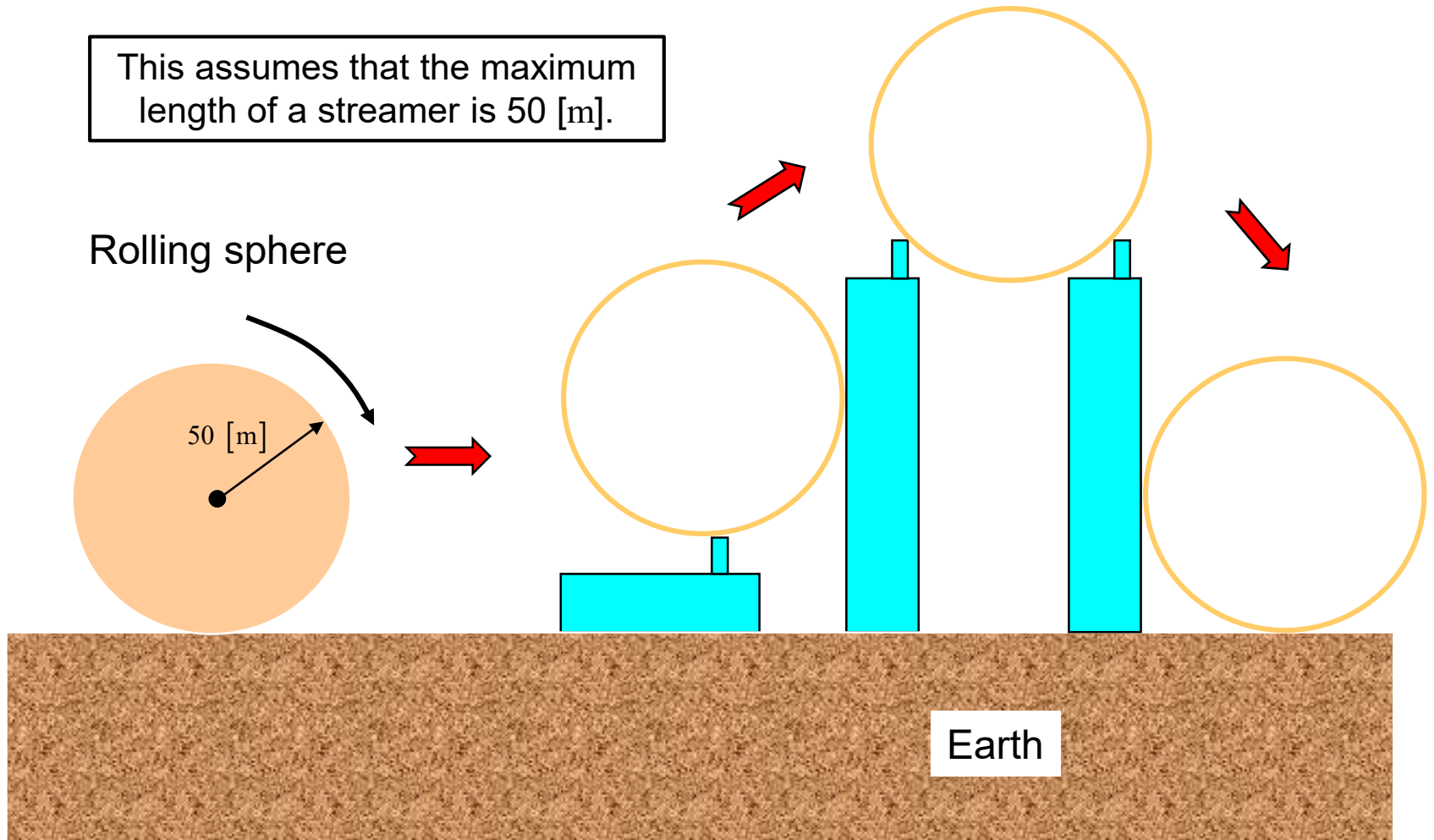
❖ Lightning may not always strike the tallest object around!



Lightning (cont.)

- ❖ The “rolling sphere” method is often used to visualize what objects are vulnerable to being struck by lightning.
- ❖ Anything the sphere touches as it rolls is subject to being hit.

This assumes that the maximum length of a streamer is 50 [m].



Ground-to-Cloud Lightning (cont.)

Ground-to-cloud lightning (note the upward forking)

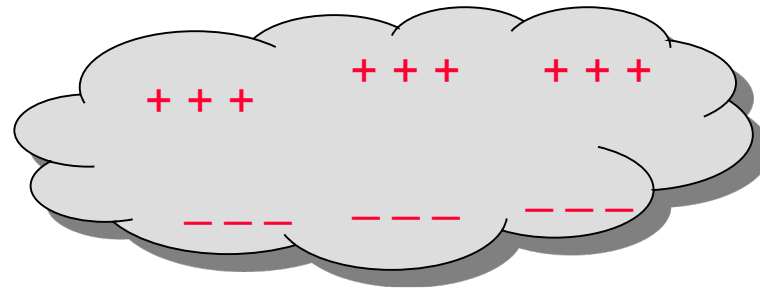


Lightning and Aircraft

- ❖ A commercial airplane is typically struck by lightning about once a year.
- ❖ The passengers are usually safe due to the “Faraday cage effect.”
- ❖ In about 10% of the cases, the airplane intercepts a leader that is traveling from the cloud (the plane “gets in the way” of the lightning).
- ❖ In about 90% of the cases, the airplane initiates the lightning strike: The leader emerges from the plane. This is often in the form of a “bi-directional leader.”
- ❖ In the bi-directional leader, a positive leader emerges from the top of the plane, and shortly after a negative leader emerges from the bottom of the plane (which is now negatively charged).

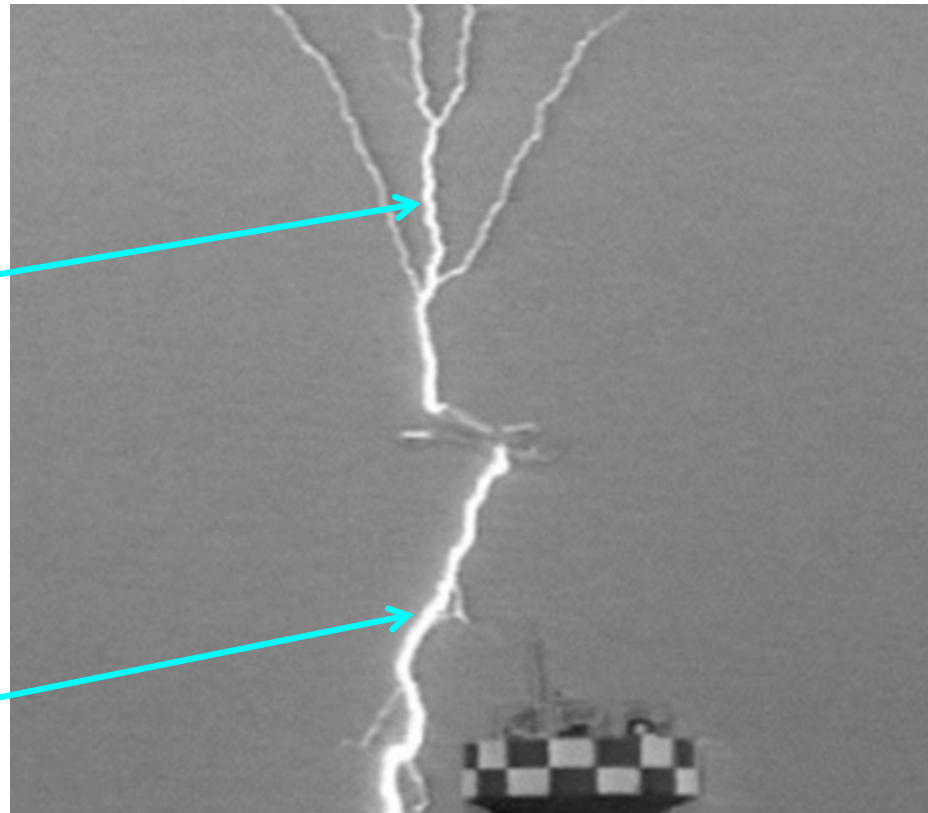
Lightning and Aircraft (cont.)

Plane “stuck” by lightning while on takeoff from the Komatsu Air Force Base off the coast in the Sea of Japan.



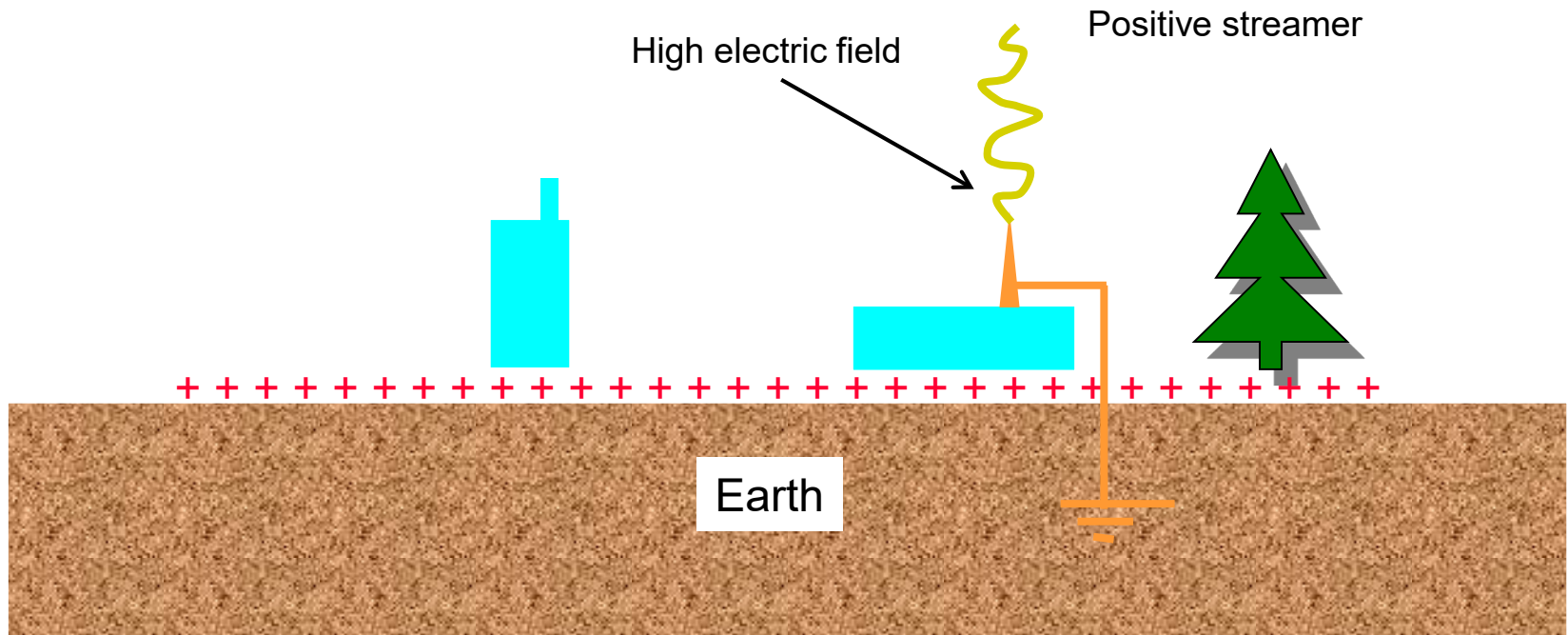
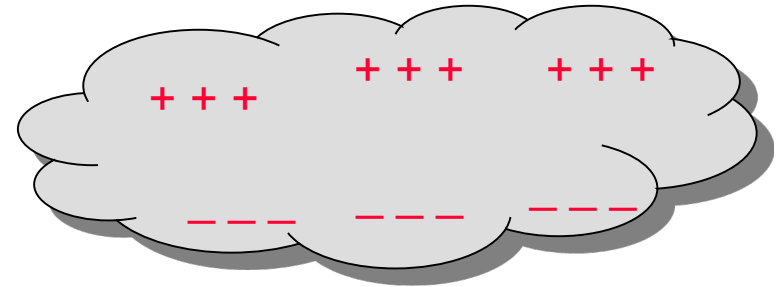
Upward-going positive leader (note upward branching)

Downward-going negative leader (note downward branching)



Lightning Rod

- A lightning rod is a rod of metal that is well grounded, and ideally fairly sharp at the end.
- The taller the better.
- It launches a good streamer (better than the surrounding points on the building) because of the high electric field near the tip.
- It should be well grounded to discharge safely a lightning strike.



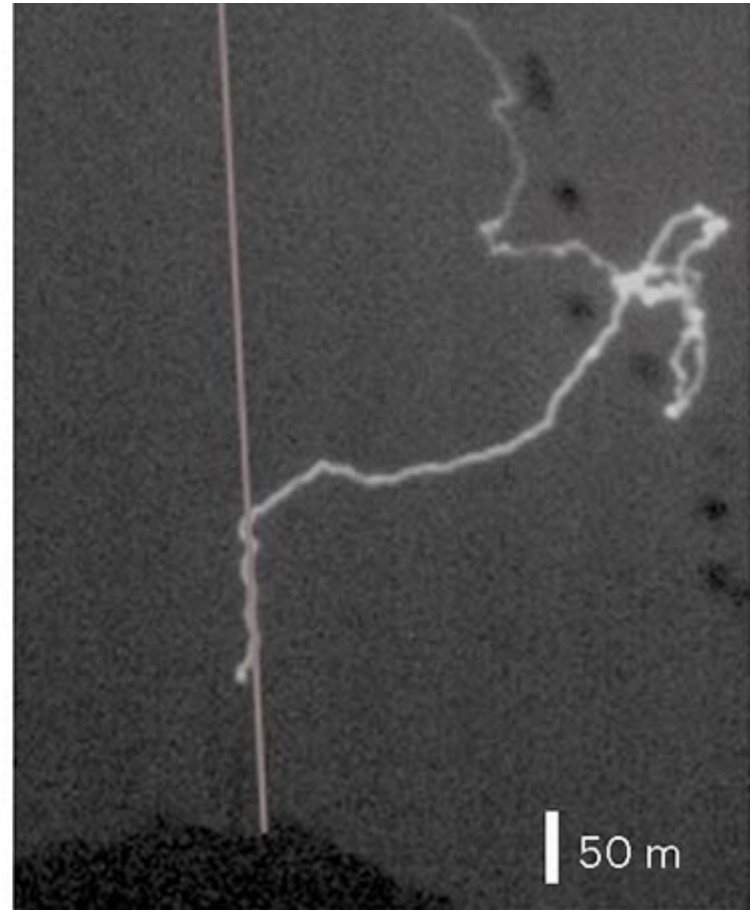
Laser Lightning Rod



Experimental study in the Swiss Alps to see if a high-power laser beam can act as a lightning rod (by ionizing the air).

Heather M. Hill, "Lightning strikes a laser rod," *Physics Today*, Jan. 25, 2023, DOI:10.1063/PT.6.1.20230125a

Laser Lightning Rod (cont.)



Results appear to be promising!

Lightning Safety

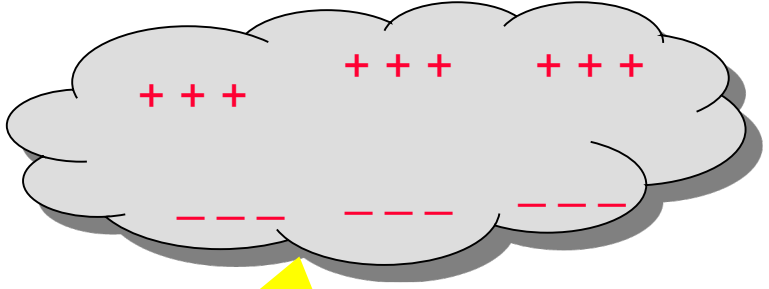
Danger exists due to:

- Direct strike from lightning
- Secondary flashover (after lightning has hit another nearby object)*
- Ground currents induced by lightning strike

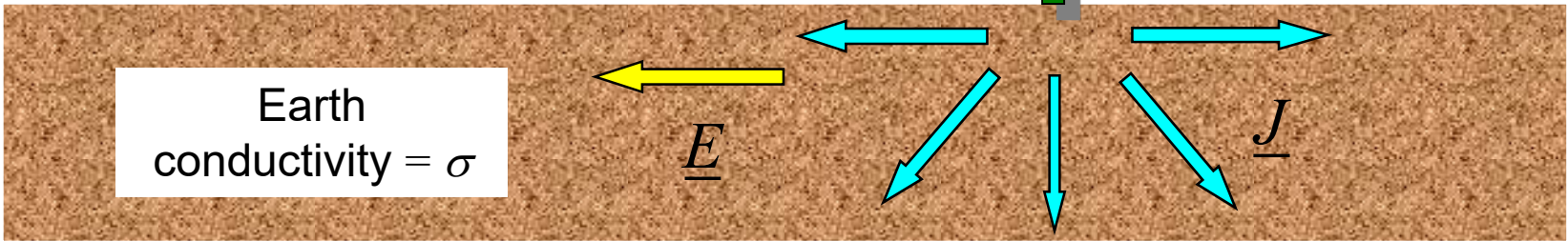
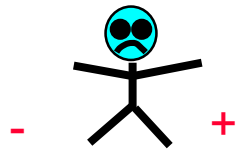
*Do not assume you are safe under a tree, just because the tree is taller than you!

Lightning Safety (cont.)

- The ground current near the strike may be very large.
- This causes an large electric field along the surface of the earth.
- It is possible to be electrocuted without being hit by the lightning.
- It is best to keep your feet together!



$$\underline{J} = \sigma \underline{E}$$
$$\underline{E} = \frac{1}{\sigma} \underline{J}$$



Lightning Safety (cont.)

Sample calculation

$$I = 20 \text{ [kA]}$$

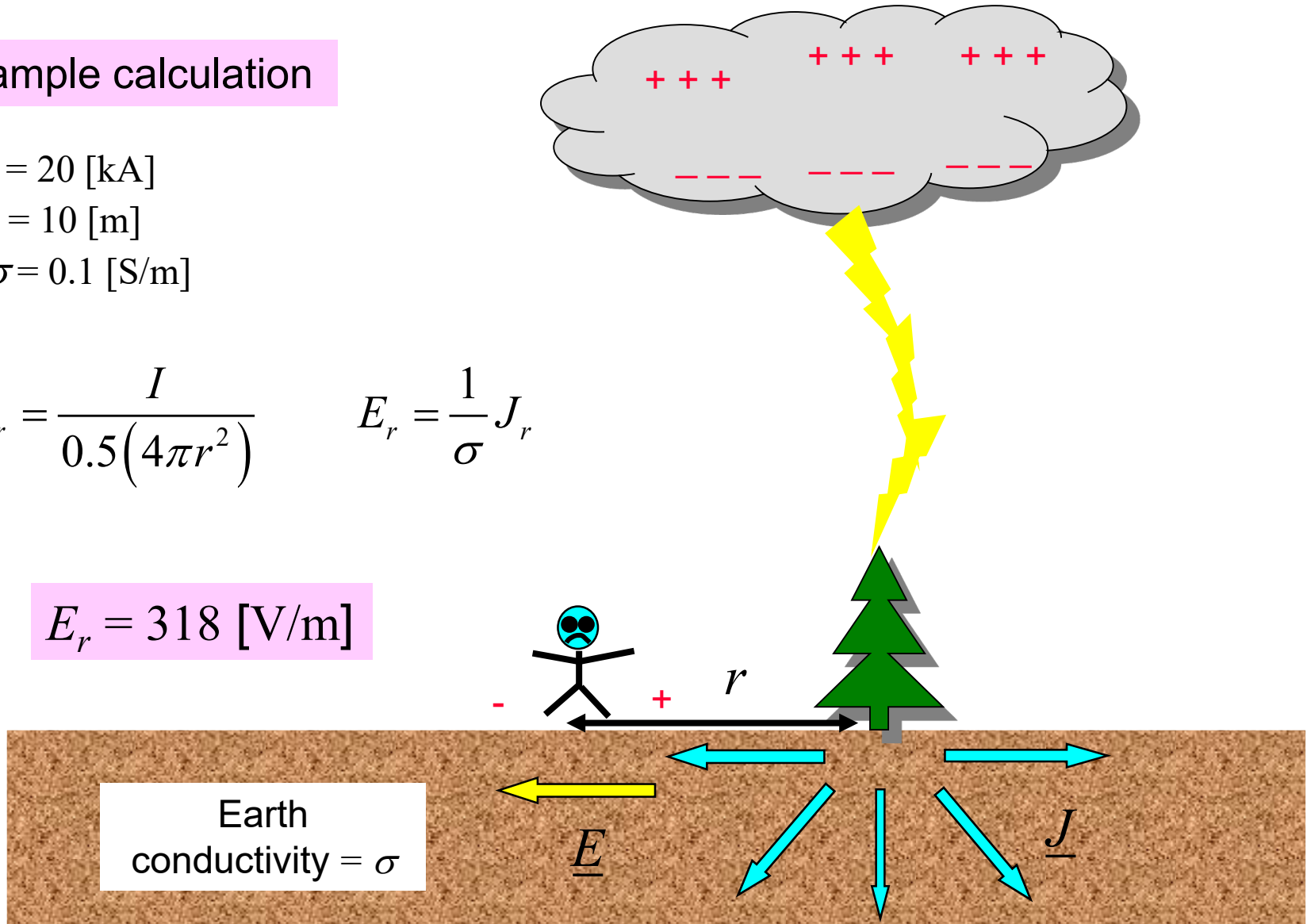
$$r = 10 \text{ [m]}$$

$$\sigma = 0.1 \text{ [S/m]}$$

$$J_r = \frac{I}{0.5(4\pi r^2)}$$

$$E_r = \frac{1}{\sigma} J_r$$

$$E_r = 318 \text{ [V/m]}$$



Lightning Safety (cont.)

Summary of Lightning Safety Rules

- 1) The best protection is to be inside of a closed metal structure such as a building or an automobile (Faraday cage effect).

- 2) If outside:
 - Make sure you are not the tallest object around.
 - Do not stand near the tallest object around (secondary flashover effect).
 - Do not carry metal poles or metal objects like golf clubs, etc. (lightning rod effect).

- 3) If you feel that a strike is imminent nearby:
 - Put your feet together, crouch down, and face away from the tallest object.

Other Lightning-like Atmospheric Discharges

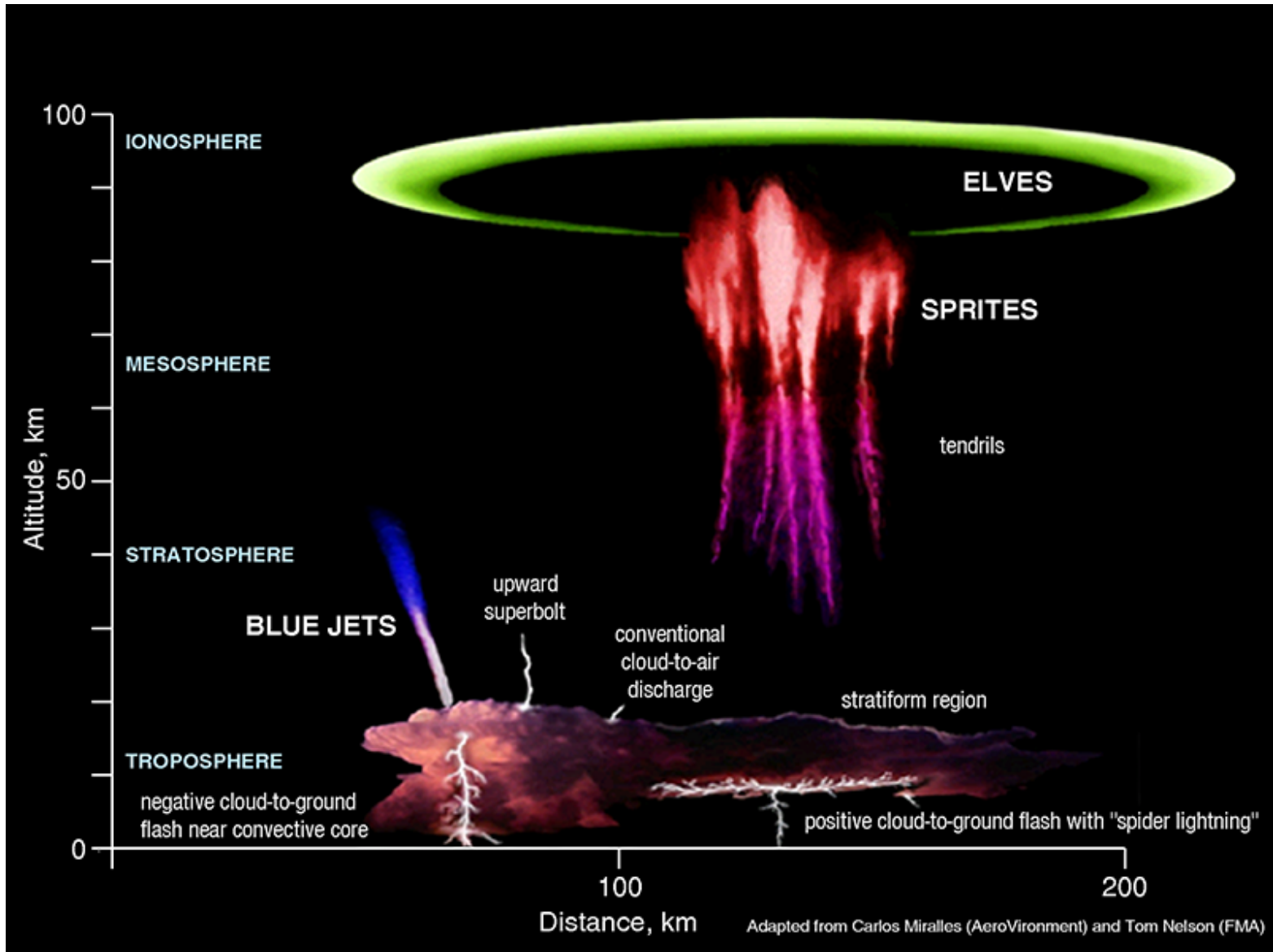
Sprites are large-scale electrical discharges that occur high above thunderstorm clouds, or cumulonimbus, giving rise to a quite varied range of visual shapes flickering in the night sky. They are triggered by the discharges of positive lightning between an underlying thundercloud and the ground. They often occur in clusters, lying 50 kilometres (31 mi) to 90 kilometres (56 mi) above the Earth's surface.

Blue jets differ from sprites in that they project from the top of the cumulonimbus above a thunderstorm, typically in a narrow cone, to the lowest levels of the ionosphere 40 to 50 km (25 to 30 miles) above the earth. In addition, whereas red sprites tend to be associated with significant lightning strikes, blue jets do not appear to be directly triggered by lightning (they do, however, appear to relate to strong hail activity in thunderstorms). They are also brighter than sprites and, as implied by their name, are blue in color.

ELVES often appear as a dim, flattened, expanding glow around 400 km (250 mi) in diameter that lasts for, typically, just one millisecond. They occur in the ionosphere 100 km (62 mi) above the ground over thunderstorms. ELVES is a whimsical acronym for **E**missions of **L**ight and **V**ery **L**ow **F**requency **P**erturbations due to **E**lectromagnetic **P**ulse **S**ources. This refers to the process by which the light is generated; the excitation of nitrogen molecules due to electron collisions (the electrons possibly having been energized by the electromagnetic pulse caused by a discharge from an underlying thunderstorm).

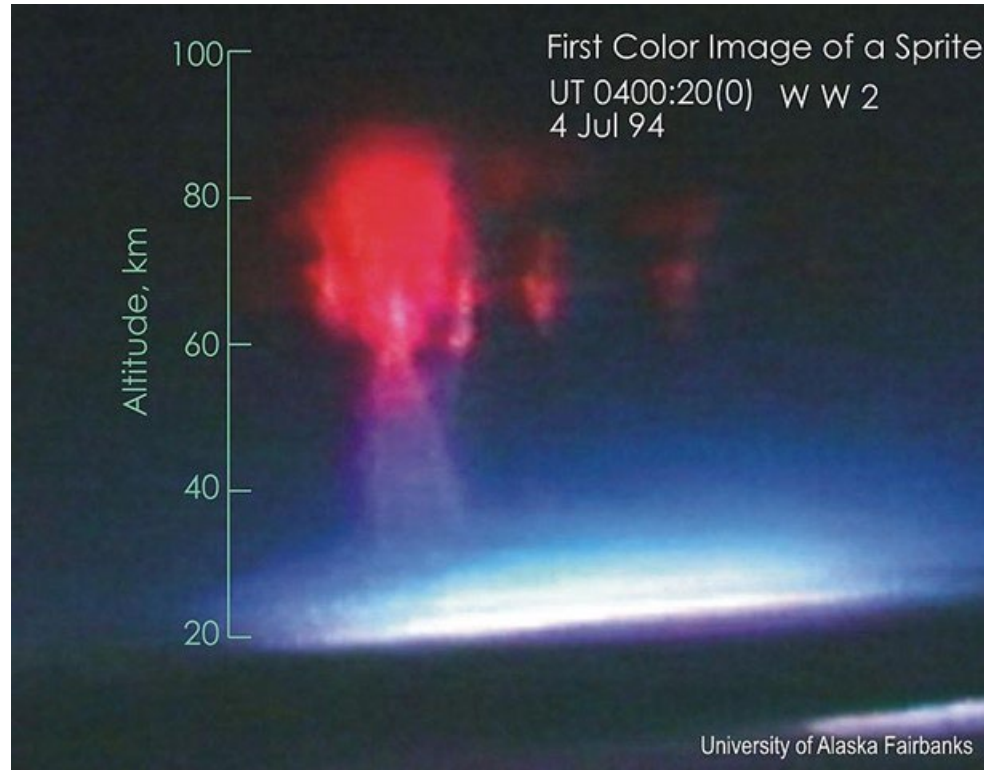
http://en.wikipedia.org/wiki/Upper-atmospheric_lightning

Other Atmospheric Discharges



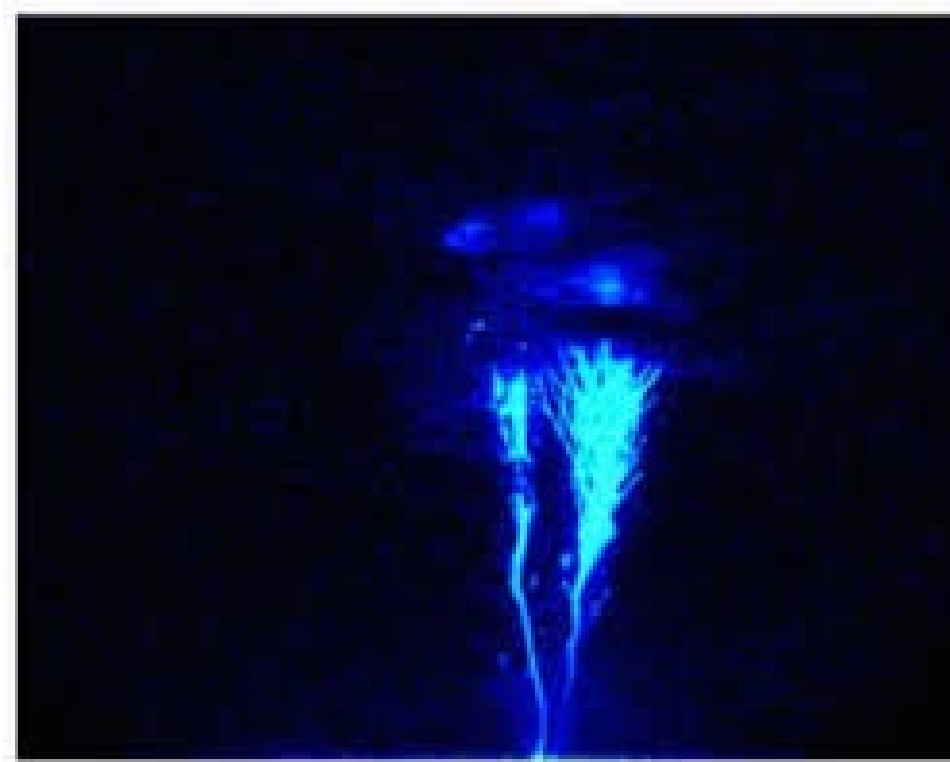
http://en.wikipedia.org/wiki/Upper-atmospheric_lightning

Atmospheric Discharges (cont.)



First color image of a sprite. It was obtained during a 1994 NASA/University of Alaska aircraft campaign to study sprites. The event was captured using an intensified color TV camera. The red color was subsequently determined to be from nitrogen fluorescent emissions excited by a lightning stroke in the underlying thunderstorm.

Atmospheric Discharges (cont.)



Blues Jets were observed for the first time in 1994. Conical jets of blue light propagate electrically from the core and are ejected from the top of the thunderstorms clouds towards the upper atmosphere at a speed of approximately 120 km/s. They usually propagate in narrow cones of 15° and do not exceed 40-50 kilometers in altitude. They are not directly related to cloud-to-ground lightnings and are not aligned with the local magnetic field.

http://en.wikipedia.org/wiki/Upper-atmospheric_lightning

Atmospheric Discharges (cont.)



An elf, as photographed in 2009 by Tim Kantola in Finland. The elf is seen together with red sprites.

<https://yle.fi/news/3-5972450>