##### DO NOT BEGIN THIS EXAM UNTIL TOLD TO START

# Name: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

#### ECE 2317

#### Applied Electricity and Magnetism

**Final Exam**

#### May 7, 2015

#### 11:00 a.m. – 2:00 p.m.

1. This exam is open-book and open-notes. A calculator is allowed (as long as it cannot be used to communicate), but no other device (laptop, phone, tablet, etc.) is allowed.
2. Show all of your work. No credit will be given if the work required to obtain the solutions is not shown.
3. Perform all your work on the exam in the space allowed.
4. Write neatly. You will not be given credit for work that is not **easily** legible.
5. Leave answers in terms of the parameters given in the problem.
6. Show units in all of your final answers.
7. Circle your final answers.
8. Double-check your answers. For simpler problems, partial credit may not be given.
9. If you have any questions, ask the instructor. You will not be given credit for work that is based on a wrong assumption.
10. Make sure you sign the academic honesty statement on the next page.

Academic Honesty Statement

I agree to abide by the UH Academic Honesty Policy during this exam. I understand that the punishment for violating this policy will be most severe, including the possibility of getting an F in the class and/or getting expelled from the University.

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Signature

Prob. 1 (30 pts.)

A parallel-plate capacitor is filled with a material having a relative permittivity of *εr*. The bottom plate is at a potential of *V*1 volts and the top plate is at a potential of *V*2 volts, with *V*2 > *V*1. Fringing at the edges of the capacitor can be neglected.

a) Solve for the potential Φ inside the parallel-plate capacitor.

b) Find the electric field vector inside the parallel-plate capacitor, using your answer to part (a).

c) Find the surface charge density on the top plate, using your answer to part (b).

d) Find the capacitance, using your answer to part (c).



ROOM FOR WORK

Prob. 2 (40 pts.)

A small metal sphere of radius *a* is suspended by a conducting wire over a large ground plane as shown below. The metal wire connects the sphere to a top plate at a potential of *V*0 volts. The center of the sphere is at a height *d* above the ground plane. The height *h* of the top plate is large enough so that the top plate can be neglected. The metal wire can also be neglected. The metal sphere is close to the ground plane, however, so that the effects of the ground plane cannot be neglected. Because the sphere is small, it can be assumed that the surface charge density on the sphere is approximately uniform.

a) Find the charge *q* on the sphere.

b) Assuming that the air surrounding the metal sphere has a breakdown field strength of *Ec*, find the maximum voltage *V*0*max* that can be placed on the metal sphere before breakdown of the air occurs. Assume that breakdown occurs at the bottom of the sphere.

c) Imagine now that the air region is replaced by a region of conductive liquid having a conductivity *σ*. What would the resistance be seen between the metal sphere and the lower plate?

ROOM FOR WORK



Prob. 3 (30 pts.)

A wire is shown below. The wire is infinite in the positive and negative *y* directions, and is located at *x* = 0. At *y* = 0 the wire changes height from *z* = 0 to *z* = *h*.

Find the magnetic field vector *H* at a point on the *z* axis that is located at a height of *z* above the origin, where *z* > *h*.



ROOM FOR WORK

Prob. 4 (30 pts.)

An infinite power line carries a low-frequency current in the *z* direction that is

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The power line is at a height of *h* above the surface of the earth. A small loop of width *w* is placed in proximity of the power line, as shown below. The center of the loop is at (*x*0, *y*0). (A separate top view of the loop is also shown for clarity, looking down from the positive y direction.) Because the earth is nonmagnetic and the frequency is low, the effects of the earth may be neglected in the calculation of the magnetic field.

a) Find the magnetic field components *Hx*, *Hy*, *Hz* at the center of the loop.

b) Find the magnetic flux *ψ* going through the loop in the upward direction, assuming that the magnetic field is approximately constant over the small dimensions of the loop.

c) Find the voltage *v*(*t*) across the output terminals of the loop.



ROOM FOR WORK

Prob. 5 (30 pts.)

An infinite wire carrying a current *I*1 in the *z* direction produces a force on a loop that is situated as shown below. The left end of the loop is at *x* = *d*, while the right end of the loop is very far away (at *x* = ∞). The loop carries a current *I*2.

Find the force vector *F* on the loop due to the infinite wire carrying current *I*1.



ROOM FOR WORK