# ECE 3455: Electronics 

Section 12071
Spring 2011

## Final Exam

Version B

May 7, 2011

Do not open the exam until instructed to do so. Answer the questions in the spaces provided on the question sheets. If you run out of room for an answer, continue on the back of the page. This is a closed-book/notes exam and you may use a calculator. You may use two crib-sheets as described in the syllabus and discussed in class. You will have 3 hours to finish the exam.

| Question | Points | Score |
| :---: | :---: | :---: |
| 1 | 30 |  |
| 2 | 30 |  |
| 3 | 20 |  |
| 4 | 20 |  |
| 5 | 20 |  |
| Total: | 120 |  |

From Table 6.2:

$$
\begin{gathered}
i_{C}=I_{S} e^{v_{B E} / V_{T}} \\
i_{B}=\frac{i_{C}}{\beta}=\left(\frac{I_{S}}{\beta}\right) e^{v_{B E} / V_{T}} \\
i_{E}=\frac{i_{C}}{\alpha}=\left(\frac{I_{S}}{\alpha}\right) e^{v_{B E} / V_{T}}
\end{gathered}
$$

Note: For the pnp transistor, replace $v_{B E}$ with $v_{E B}$.

$$
\begin{gathered}
i_{C}=\alpha i_{E} \\
i_{C}=\beta i_{B} \\
\beta=\frac{\alpha}{1-\alpha} \\
i_{B}=(1-\alpha) i_{E}=\frac{i_{E}}{\beta+1} \\
i_{E}=(\beta+1) i_{B} \\
\alpha=\frac{\beta}{\beta+1}
\end{gathered}
$$

$V_{T}=$ thermal voltage $=\frac{k T}{q} \simeq 25 \mathrm{mV}$ at room temperature

## Summary of Table 6.4 (Small Signal Model Parameters)

Model Parameters in Terms of DC Bias Currents
$g_{m}=\frac{I_{C}}{V_{T}} \quad r_{e}=\frac{V_{T}}{I_{E}}=\alpha \frac{V_{T}}{I_{C}} \quad r_{\pi}=\frac{V_{T}}{I_{B}}=\beta \frac{V_{T}}{I_{C}} \quad r_{o}=\frac{\left|V_{A}\right|}{I_{C}}$
In Terms of $g_{m}$
$r_{e}=\frac{\alpha}{g_{m}} \quad r_{\pi}=\frac{\beta}{g_{m}}$
In Terms of $r_{e}$

$$
g_{m}=\frac{\alpha}{r_{e}} \quad r_{\pi}=(\beta+1) r_{e} \quad g_{m}+\frac{1}{r_{\pi}}=\frac{1}{r_{e}}
$$

1. (30 points) A customer asks you to design a circuit that has the following frequency response (a straight-line approximation of its magnitude) using only ideal op-amps, capacitors (any value), and $10 \mathrm{k} \Omega$ and $100 \mathrm{k} \Omega$ resistors.

(a) Write a possible transfer function $H(j \omega)$ in terms of 3 dB corner frequencies that are labeled as $\omega_{1}, \omega_{2}$, etc.
(b) Break the transfer function up into components that you can construct as circuits.
(c) Design the sub-circuits.
(d) Indicate how the sub-circuits fit together to make your complete circuit.
2. (30 points) The following circuit is a phase splitter. For your solutions, you must first show a series of expressions (each boxed in) and then you may calculate a numerical answer. For example, you may find $V_{\mathrm{BB}}$ as a function of resistors and power supply voltages and then box in this expression. You may then use $V_{\mathrm{BB}}$ in subsequent expressions.
(a) Complete the DC analysis of this circuit and confirm that the circuit is in active mode.
(b) Sketch the circuit for the small signal analysis.
(c) Find an expression for the bandpass gain $v_{c} / v_{i n}$ and calculate its value. Please note that you are to find $v_{c} / v_{i n}$, not $v_{c} / v_{s}$.
(d) Find an expression for the bandpass gain $v_{e} / v_{i n}$ and calculate its value.
(e) Find an expression for the bandpass values for $R_{\text {in }}, R_{\text {outC }}$ (at the collector), and $R_{\text {outE }}$ (at the emitter), and calculate their values.
(f) Compare the gains at the two output terminals and explain why this is called a phase splitter.


Important: From the next three questions, complete any two. You must indicate which one should not be graded by clearly marking Do not grade on the page or else I will not grade the last problem.
3. (20 points) In the following circuit, it is much easier to find a solution if we apply Miller's theorem to move the resistor $R_{f}$. Remember that for the Miller theorem, $R_{M i}=\frac{R}{1-K}$ and $R_{M o}=\frac{R}{1-\frac{1}{K}}$, where $K$ is the voltage gain between the component to be substituted. To make this easier, take advantage of the fact that $R_{f} \gg R_{2}| | R_{L}$ and ignore the current flowing through $R_{f}$ when finding $K$.

(a) Find $K$.
(b) Find $R_{M i}$ and $R_{M o}$ and sketch the new circuit.
(c) Find $\frac{v_{\text {out }}}{v_{S}}$ for the bandpass as indicated on the circuit.
(d) You cannot use this modified circuit to determine $R_{\text {out }}$. Why not?
(e) Find $R_{\text {in }}$ and $R_{\text {out }}$.
4. (a) (10 points) For the circuit below, plot $v_{A}$ and $v_{B}$ for

$$
v_{I N}=V_{o} \sin \left(\omega_{0} t\right),
$$

where $V_{o}=5$ volts and
i. $\omega_{0}=100 \mathrm{rad} / \mathrm{s}$.
ii. $\omega_{0}=10,000 \mathrm{rad} / \mathrm{s}$.

Place your sketches for $v_{A}$ and $v_{B}$ on the same plot and make one plot for each frequency. Assume a constant voltage drop model for the diodes with $V_{D}=0.7$ volts, $V_{Z}=4$ volts, and an ideal op-amp. Be sure to label your graph to receive credit. Hint: For the constant voltage drop model, the Zener diode internal resistance can be neglected.

(b) (10 points) For the following circuit,
i. Sketch $V_{O U T}$ vs. $V_{I N}$ on the first graph provided.
ii. Sketch $V_{\text {OUT }}(t)$ on the second graph alongside the sketch of $V_{I N}(t)$.



5. (20 points) For the following circuit,
(a) Sketch the circuit for the small signal analysis (do not do a DC analysis - leave everything in terms of the circuit resistors, $\beta$, and $r_{\pi}$ ).
(b) Find an expression for the bandpass gain of the circuit.
(c) Find expressions for $R_{\text {in }}$ and $R_{\text {out }}$ as indicated on the circuit in the bandpass.


