

When the bit is 0, the switch is in the position labeled 0; when the bit is 1, the switch is in the position labeled 1. The analog output is the current i_o . V_{ref} is a constant reference voltage.

(a) Show that

$$i_o = \frac{V_{ref}}{R} \left(\frac{b_1}{2^1} + \frac{b_2}{2^2} + \dots + \frac{b_N}{2^N} \right)$$

- (b) Which bit is the LSB? Which is the MSB?
 (c) For $V_{ref} = 10$ V, $R = 10$ k Ω , and $N = 8$, find the maximum value of i_o obtained. What is the change in i_o resulting from the LSB changing from 0 to 1?

1.38 In compact-disc (CD) audio technology, the audio signal is sampled at 44.1 kHz. Each sample is represented by 16 bits. What is the speed of this system in bits per second?

Section 1.4: Amplifiers

1.39 Various amplifier and load combinations are measured as listed below using rms values. For each, find the voltage, current, and power gains (A_v , A_i , and A_p , respectively) both as ratios and in dB:

- (a) $v_i = 100$ mV, $i_i = 100$ μ A, $v_o = 10$ V, $R_L = 100$ Ω
 (b) $v_i = 10$ μ V, $i_i = 100$ nA, $v_o = 1$ V, $R_L = 10$ k Ω
 (c) $v_i = 1$ V, $i_i = 1$ mA, $v_o = 5$ V, $R_L = 10$ Ω

1.40 An amplifier operating from ± 3 -V supplies provides a 2.2-V peak sine wave across a 100- Ω load when provided with a 0.2-V peak input from which 1.0 mA peak is drawn. The average current in each supply is measured to be 20 mA. Find the voltage gain, current gain, and power gain expressed as ratios and in decibels as well as the supply power, amplifier dissipation, and amplifier efficiency.

1.41 An amplifier using balanced power supplies is known to saturate for signals extending within 1.0 V of either supply. For linear operation, its gain is 200 V/V. What is the rms value of the largest undistorted sine-wave output available, and input needed, with ± 5 -V supplies? With ± 10 -V supplies? With ± 15 -V supplies?

1.42 Symmetrically saturating amplifiers, operating in the so-called clipping mode, can be used to convert sine waves to pseudo-square waves. For an amplifier with a small-signal gain of 1000 and clipping levels of ± 10 V, what peak value of input sinusoid is needed to produce an output whose extremes are just at the edge of clipping? Clipped 90% of the time? Clipped 99% of the time?

Section 1.5: Circuit Models for Amplifiers

1.43 Consider the voltage-amplifier circuit model shown in Fig. 1.16(b), in which $A_{vo} = 100$ V/V under the following conditions:

- (a) $R_i = 10R_s$, $R_L = 10R_o$
 (b) $R_i = R_s$, $R_L = R_o$
 (c) $R_i = R_s/10$, $R_L = R_o/10$

Calculate the overall voltage gain v_o/v_s in each case, expressed both directly and in decibels.

1.44 An amplifier with 40 dB of small-signal, open-circuit voltage gain, an input resistance of 1 M Ω , and an output resistance of 100 Ω , drives a load of 500 Ω . What voltage and power gains (expressed in dB) would you expect with the load connected? If the amplifier has a peak output-current limitation of 20 mA, what is the rms value of the largest sine-wave input for which an undistorted output is possible? What is the corresponding output power available?

1.45 A 10-mV signal source having an internal resistance of 100 k Ω is connected to an amplifier for which the input resistance is 10 k Ω , the open-circuit voltage gain is 1000 V/V, and the output resistance is 1 k Ω . The amplifier is connected in turn to a 100- Ω load. What overall voltage gain results as measured from the source internal voltage to the load? Where did all the gain go? What would the gain be if the source was connected directly to the load? What is the ratio of these two gains? This ratio is a useful measure of the benefit the amplifier brings.

1.46 A buffer amplifier with a gain of 1 V/V has an input resistance of 1 M Ω and an output resistance of 20 Ω . It is connected between a 1-V, 200-k Ω source and a 100- Ω

load. What load voltage results? What are the corresponding voltage, current, and power gains (in dB)?

✓ **1.47** Consider the cascade amplifier of Example 1.3. Find the overall voltage gain v_o/v_i obtained when the first and second stages are interchanged. Compare this value with the result in Example 1.3, and comment.

✓ **1.48** You are given two amplifiers, A and B, to connect in cascade between a 10-mV, 100-k Ω source and a 100- Ω load. The amplifiers have voltage gain, input resistance, and output resistance as follows: for A, 100 V/V, 100 k Ω , 10 k Ω , respectively; for B, 10 V/V, 10 k Ω , 1 k Ω , respectively. Your problem is to decide how the amplifiers should be connected. To proceed, evaluate the two possible connections between source S and load L, namely, SABL and SBAL. Find the voltage gain for each both as a ratio and in decibels. Which amplifier arrangement is best?

D *1.49 A designer has available voltage amplifiers with an input resistance of 10 k Ω , an output resistance of 1 k Ω , and an open-circuit voltage gain of 10. The signal source has a 10-k Ω resistance and provides a 5-mV rms signal, and it is required to provide a signal of at least 3 V rms to a 200- Ω load. How many amplifier stages are required? What is the output voltage actually obtained?

✓ **D *1.50** Design an amplifier that provides 0.5 W of signal power to a 100- Ω load resistance. The signal source provides a 30-mV rms signal and has a resistance of 0.5 M Ω . Three types of voltage-amplifier stages are available:

- A high-input-resistance type with $R_i = 1 \text{ M}\Omega$, $A_{vo} = 10$, and $R_o = 10 \text{ k}\Omega$
- A high-gain type with $R_i = 10 \text{ k}\Omega$, $A_{vo} = 100$, and $R_o = 1 \text{ k}\Omega$
- A low-output-resistance type with $R_i = 10 \text{ k}\Omega$, $A_{vo} = 1$, and $R_o = 20 \Omega$

Design a suitable amplifier using a combination of these stages. Your design should utilize the minimum number of stages and should ensure that the signal level is not reduced below 10 mV at any point in the amplifier chain. Find the load voltage and power output realized.

D *1.51 It is required to design a voltage amplifier to be driven from a signal source having a 5-mV peak amplitude and a source resistance of 10 k Ω to supply a peak output of 2 V across a 1-k Ω load.

- What is the required voltage gain from the source to the load?
- If the peak current available from the source is 0.1 μA , what is the smallest input resistance allowed? For the design with this value of R_i , find the overall current gain and power gain.
- If the amplifier power supply limits the peak value of the output open-circuit voltage to 3 V, what is the largest output resistance allowed?
- For the design with R_i as in (b) and R_o as in (c), what is the required value of open-circuit voltage gain, i.e., $\left. \frac{v_o}{v_i} \right|_{R_L \rightarrow \infty}$, of the amplifier?
- If, as a possible design option, you are able to increase R_i to the nearest value of the form $1 \times 10^n \Omega$ and to decrease R_o to the nearest value of the form $1 \times 10^m \Omega$, find (i) the input resistance achievable; (ii) the output resistance achievable; and (iii) the open-circuit voltage gain now required to meet the specifications.

D 1.52 A voltage amplifier with an input resistance of 20 k Ω , an output resistance of 100 Ω , and a gain of 1000 V/V is connected between a 100-k Ω source with an open-circuit voltage of 10 mV and a 100- Ω load. For this situation:

- What output voltage results?
- What is the voltage gain from source to load?
- What is the voltage gain from the amplifier input to the load?
- If the output voltage across the load is twice that needed and there are signs of internal amplifier overload, suggest the location and value of a single resistor that would produce the desired output. Choose an arrangement that would cause minimum disruption to an operating circuit. (*Hint:* Use parallel rather than series connections.)

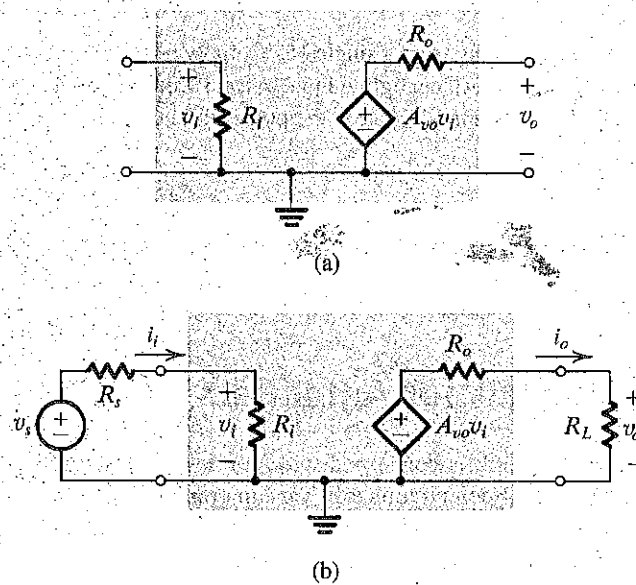


Figure 1.16 (a) Circuit model for the voltage amplifier, (b) The voltage amplifier with input signal source and load.

calculated. If a load resistance is not specified, it is normally assumed that the given voltage gain is the open-circuit gain A_{vo} .

The finite input resistance R_i introduces another voltage-divider action at the input, with the result that only a fraction of the source signal v_s actually reaches the input terminals of the amplifier; that is,

$$v_i = v_s \frac{R_i}{R_i + R_s} \quad (1.13)$$

It follows that in order not to lose a significant portion of the input signal in coupling the signal source to the amplifier input, the amplifier must be designed to have an input resistance R_i much greater than the resistance of the signal source, $R_i \gg R_s$. Furthermore, there are applications in which the source resistance is known to vary over a certain range. To minimize the effect of this variation on the value of the signal that appears at the input of the amplifier, the design ensures that R_i is much greater than the largest value of R_s . An ideal voltage amplifier is one with $R_i = \infty$. In this ideal case both the current gain and power gain become infinite.

The overall voltage gain (v_o/v_s) can be found by combining Eqs. (1.12) and (1.13),

$$\frac{v_o}{v_s} = A_{vo} \frac{R_i}{R_i + R_s} \frac{R_L}{R_L + R_o}$$

There are situations in which one is interested not in voltage gain but only in a significant power gain. For instance, the source signal can have a respectable voltage but a source resistance that is much greater than the load resistance. Connecting the source directly to the load would result in significant signal attenuation. In such a case, one requires an amplifier with a high input resistance (much greater than the source resistance) and a low output resistance (much smaller than the load resistance) but with a modest voltage gain (or even unity gain).