ECE 6345 Spring 2015

Homework 5

- 1) A rectangular microstrip antenna is printed on a lossless substrate having a substrate relative permittivity $\varepsilon_r = 2.2$. The aspect ratio of the patch is W/L = 1.5. The antenna is operated at the resonant frequency (assume that fringing may be ignored, so the length of the patch is one-half of a wavelength in the dielectric). Plot the exact Q_{sp} versus the normalized substrate thickness h / λ_0 over the range $0 < h / \lambda_0 < 0.1$. On the same graph, add a plot of the CAD result for Q_{sp} (which involves the CAD formula for *p*). The exact Q_{sp} is based on the exact P_{sp} , which comes from the exact power radiated by the equivalent dipole (which involves a single integration in θ) and the exact *p* factor (which must be found from a double integration in θ and ϕ .
- 2) Redo the above problem for a substrate relative permittivity of 10.8.
- 3) Consider the rectangular patch of Prob. 1. Plot the exact directivity (dB) versus the normalized substrate thickness h / λ_0 over the range $0 < h / \lambda_0 < 0.1$. On the same graph, add a plot of the CAD results for the directivity (from a closed-form expression, which uses the CAD formula for *p*).
- 4) Redo the previous problem for a substrate relative permittivity of 10.8.
- 5) A circular microstrip antenna is printed on a lossless substrate having a substrate relative permittivity $\varepsilon_r = 2.2$. The antenna is operated at the resonance frequency of the TM₀₁₁ mode. Ignore fringing, so that

 $a = 0.29304 \,\lambda_0 \,/ \sqrt{\varepsilon_r} \,.$

Plot the exact Q_{sp} versus the normalized substrate thickness h / λ_0 over the range $0 < h / \lambda_0 < 0.1$. On the same graph, add a plot of the CAD result for Q_{sp} (which uses the CAD formulas for p and I_0). The exact Q_{sp} must be found from a numerical integration in θ .

- 6) Redo the previous problem for a substrate relative permittivity of 10.8.
- 7) Consider the circular patch of Prob. 4. Plot the exact directivity (dB) versus the normalized substrate thickness h / λ_0 over the range $0 < h / \lambda_0 < 0.1$. On the same graph, add a plot of the CAD result for the directivity (from a closed-form expression, which uses the CAD formula for *p*).
- 8) Repeat the previous problem using a substrate permittivity of 10.8.